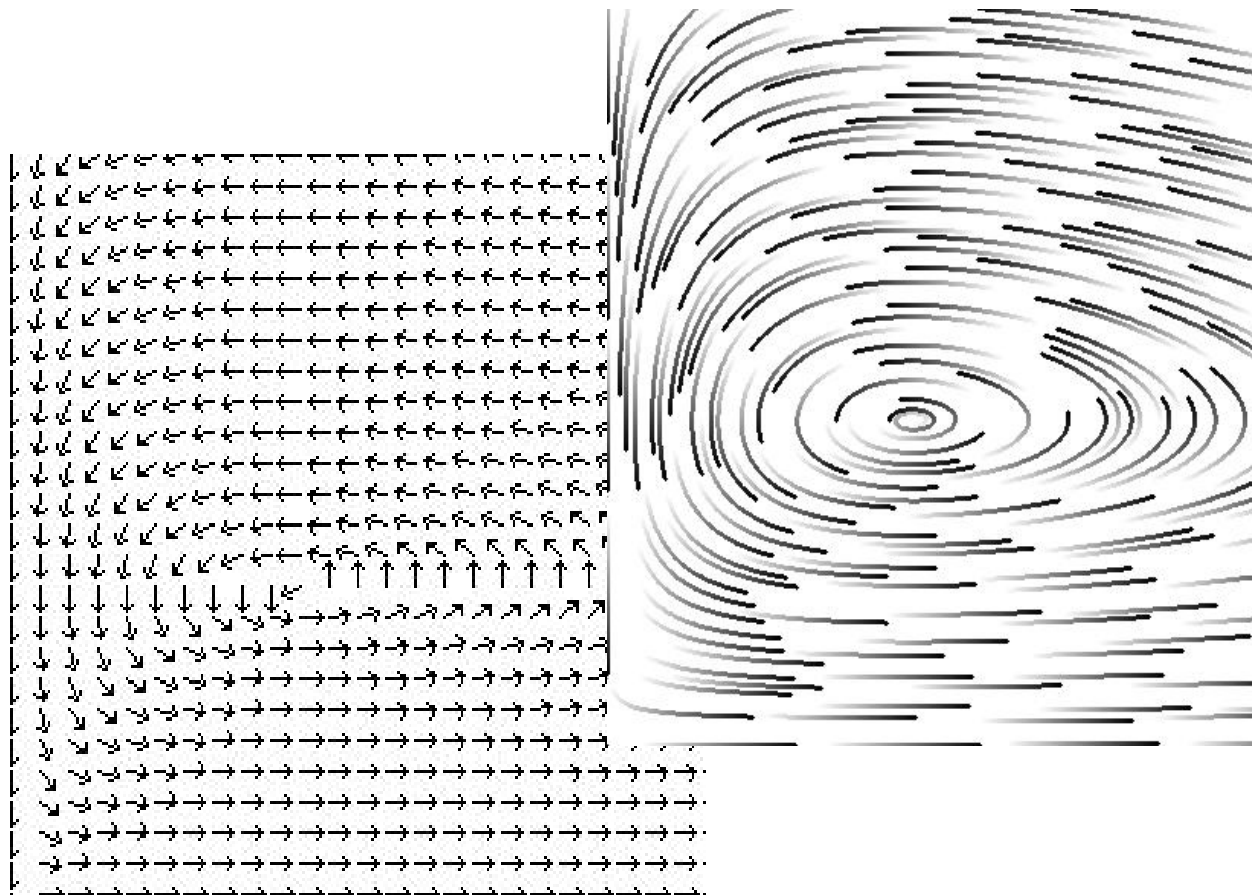


Arrows vs. Streamlines vs. Textures

Streamlines: selective

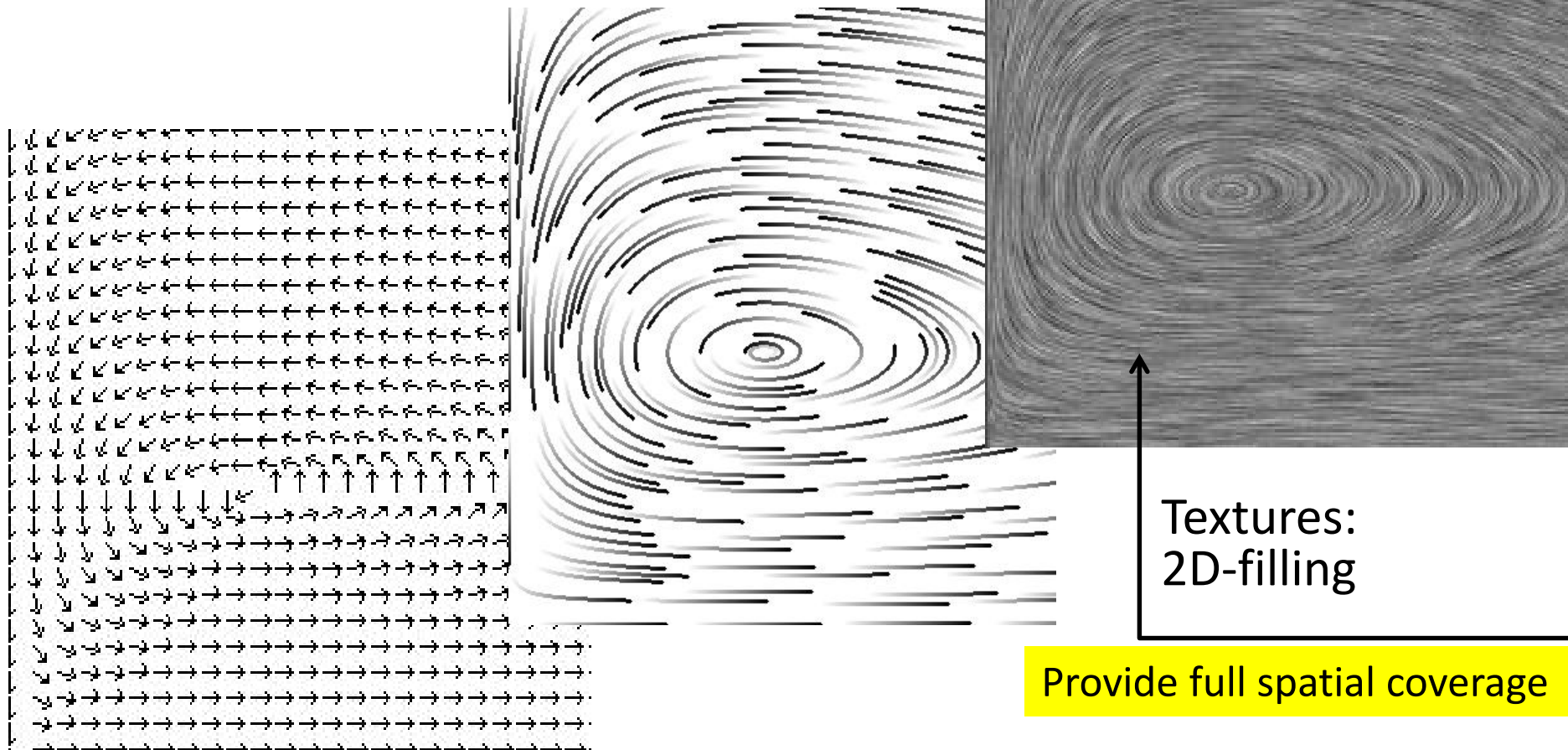
Arrows: simple



Arrows vs. Streamlines vs. Textures

Streamlines: selective

Arrows: simple



Textures:
2D-filling

Provide full spatial coverage

Vector Field Visualization: Texture-based Method

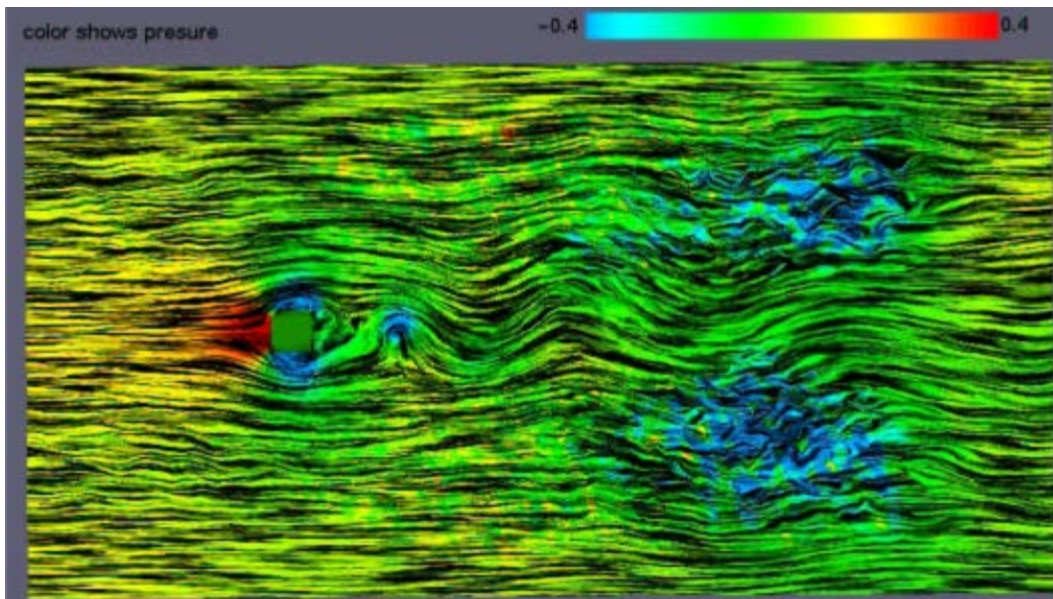
Goal: understand the basic idea behind texture-based method (no need to remember all techniques); understand the mechanism of LIC and IBFV; be able to implement LIC

A BRIEF OVERVIEW

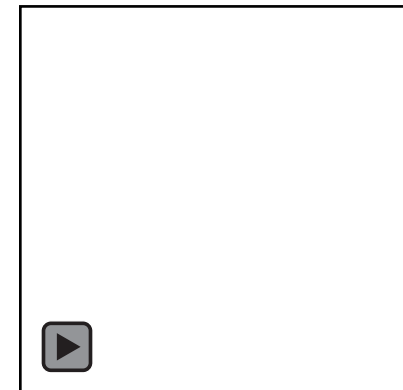
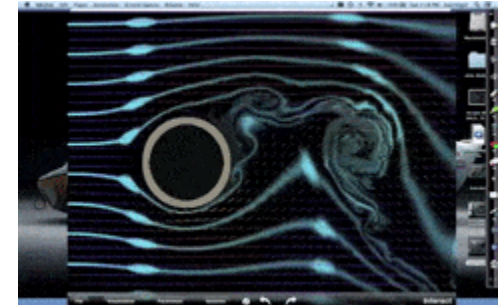
Overview — Texture-Based Methods

➤ Spot Noise

- ✧ **One of the first texture-based** techniques (*Van Wijk, Siggraph1991*).
- ✧ **Basic idea:** *distribute a set of intensity function, or spot, over the domain, that is wrapped by the flow over a small step.*
- ✧ **Pro:** mimic the smear effect of oil; encode magnitude; can be applied for both steady and unsteady flow.
- ✧ **Con:** tricky to implement; low quality; computationally expensive.



[De Leeuw and Van Liere]



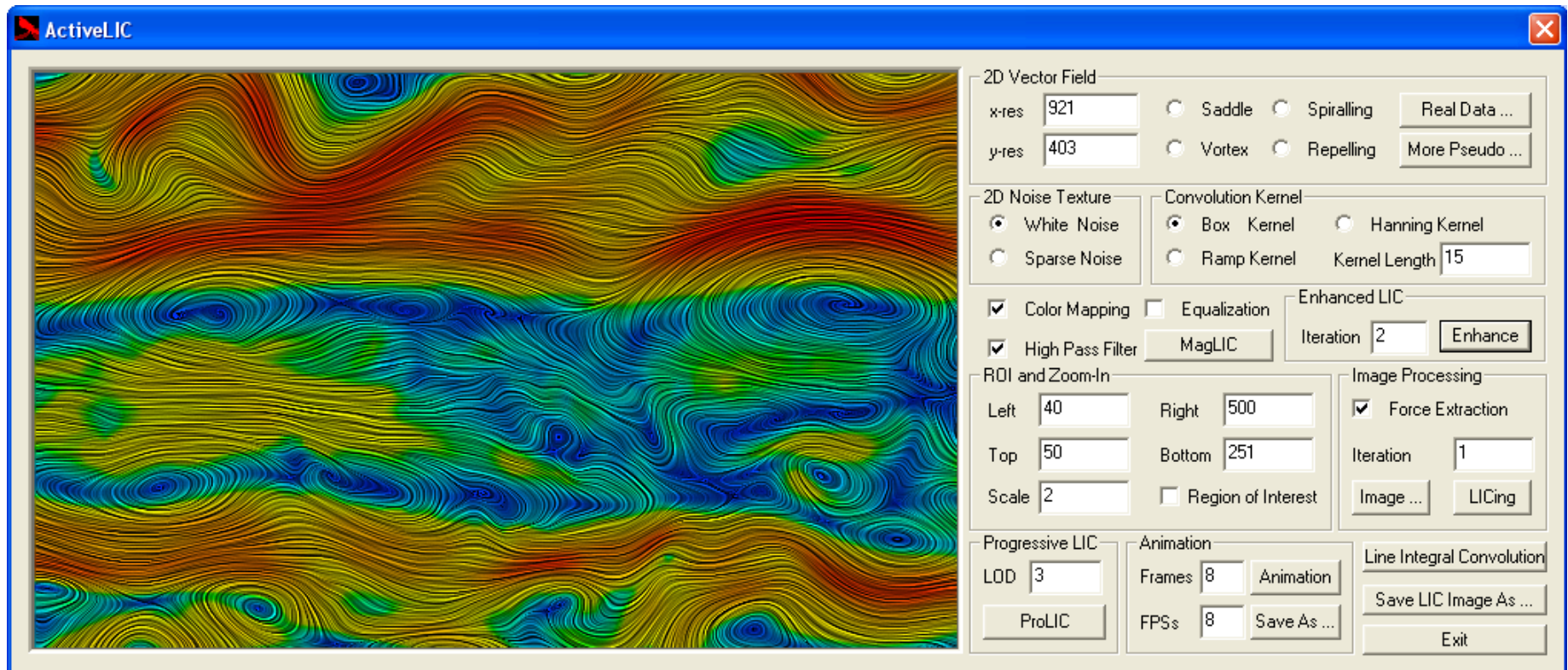


Overview — Texture-Based Methods

Line Integral Convolution (LIC)

pixel-based

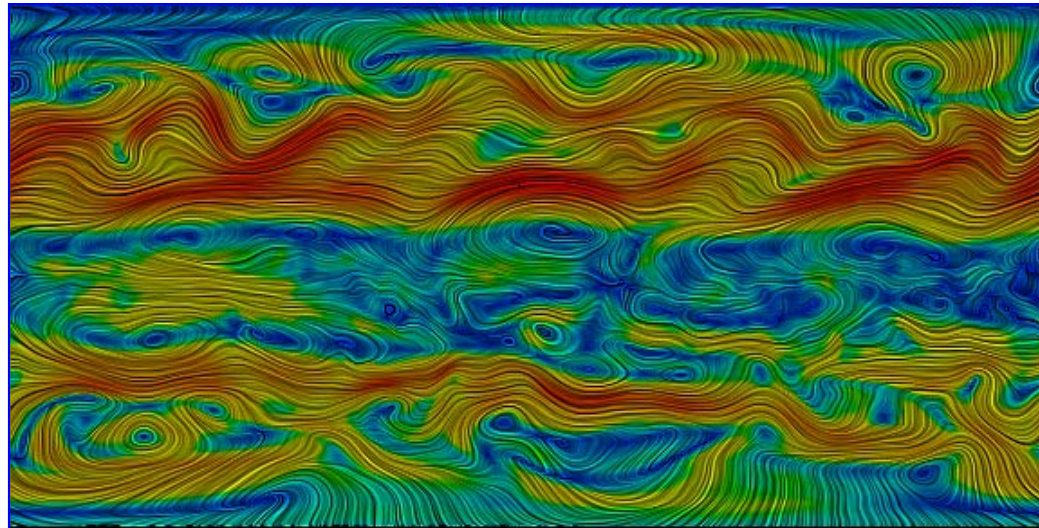
- ✧ One of the most popular techniques (*Brian Cabral & Leith Leedom, SIGGRAPH93*).
- ✧ **Basic idea:** *Low-pass filters white noise* along pixel-centered symmetrically bi-directional **streamlines** to exploit spatial correlation in the flow direction.
- ✧ **Pro:** High-quality image with fine features; easy implementation; and many variants.
- ✧ **Con:** Computationally expensive; limited to steady flow visualization.



Overview — Texture-Based Methods

➤ Unsteady Flow LIC (UFLIC)

- ✧ The first texture-based **unsteady** flow visualization method (by *Han-Wei Shen and David Kao, IEEE Visualization 97 & IEEE TVCG 98*).
- ✧ **Basic idea:** Time-accurately scatters particle values of *successively fed-forward textures* along *pathlines* over several time steps to convey the footprint / contribution that a particle leaves at downstream locations as the flow runs forward.
- ✧ **Pro:** High temporal coherence & high spatial coherence & hardware-independent.
- ✧ **Con:** Low computational performance due to *multi-step* (≈ 100) *pathline integration*.

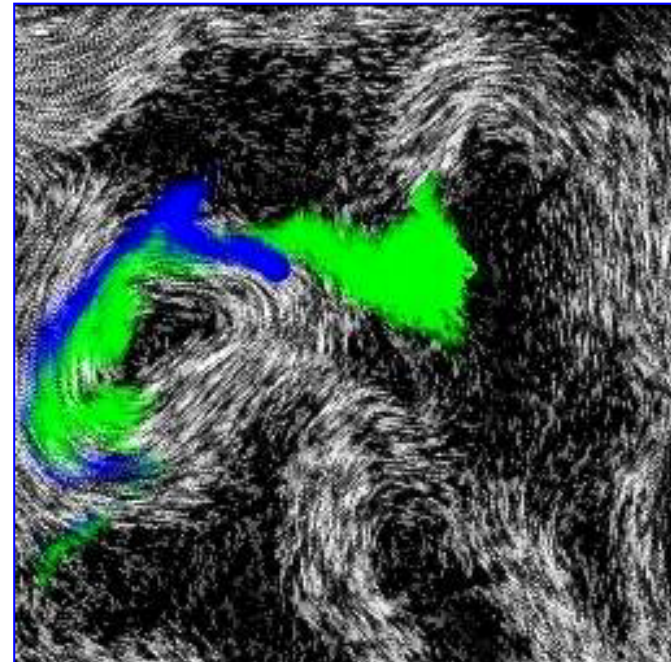
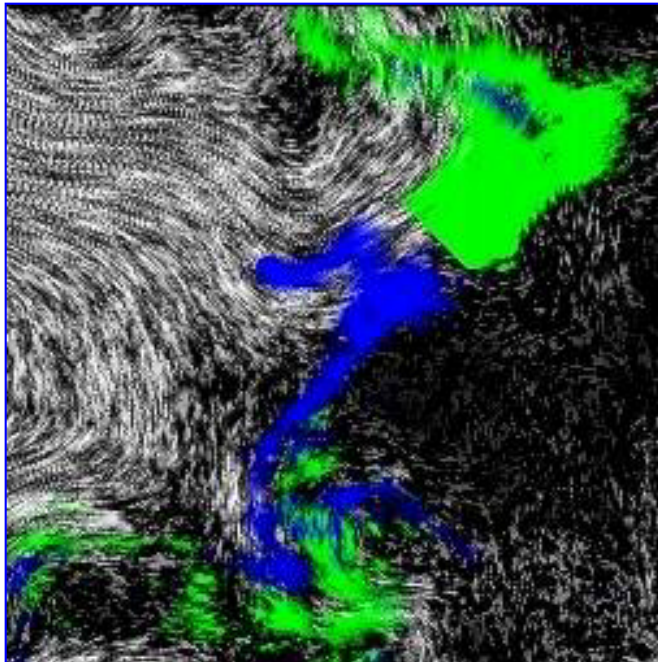


Overview — Texture-Based Methods

➤ Hardware-Accelerated Texture Advection (HATA)

- ✧ The **first hardware-based** texture synthesis technique for unsteady flow (by Bruno Jobard and et al., *IEEE Visualization 00*).
- ✧ **Basic idea:** Exploits *indirect pixel-texture addressing* for fast flow advection, & additive / subtractive texture blending for fast texture convolution in an efficient pipeline.
- ✧ **Pro:** Near-interactive frame rates based on special-purpose graphics cards; for both steady and unsteady flow; good temporal coherence .
- ✧ **Con:** poor spatial coherence (very noisy).

exponential kernel

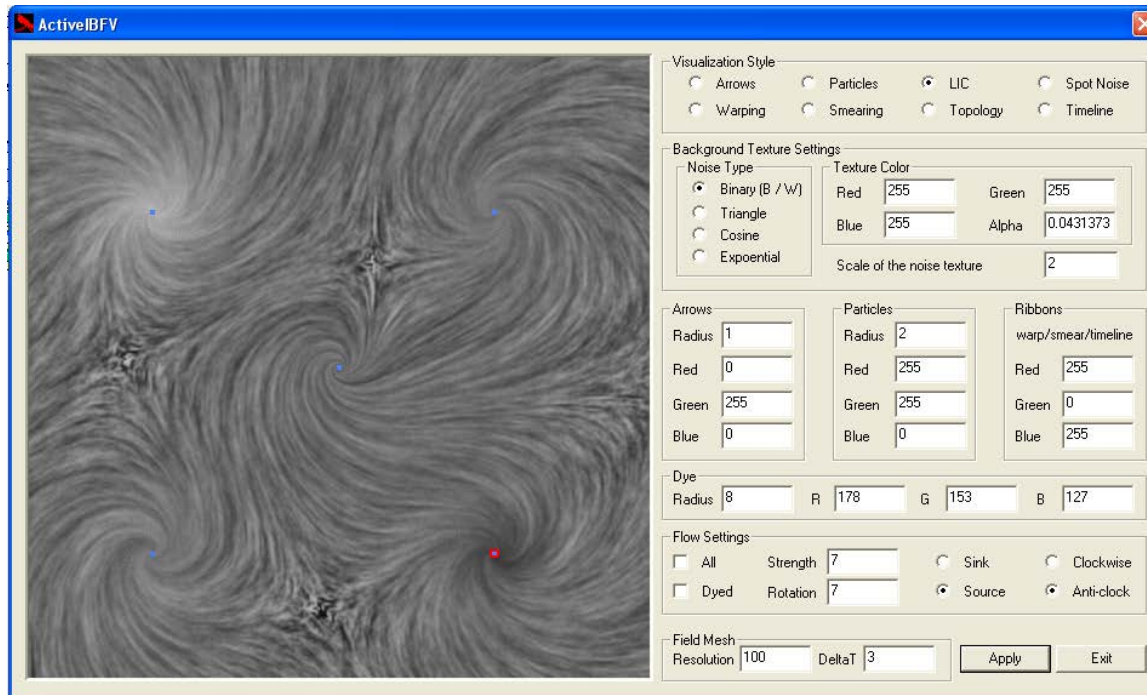


(Bruno Jobard, Gordon Erlebacher, and M. Yousuff Hussaini)

Overview — Texture-Based Methods

➤ Image-Based Flow Visualization (IBFV)

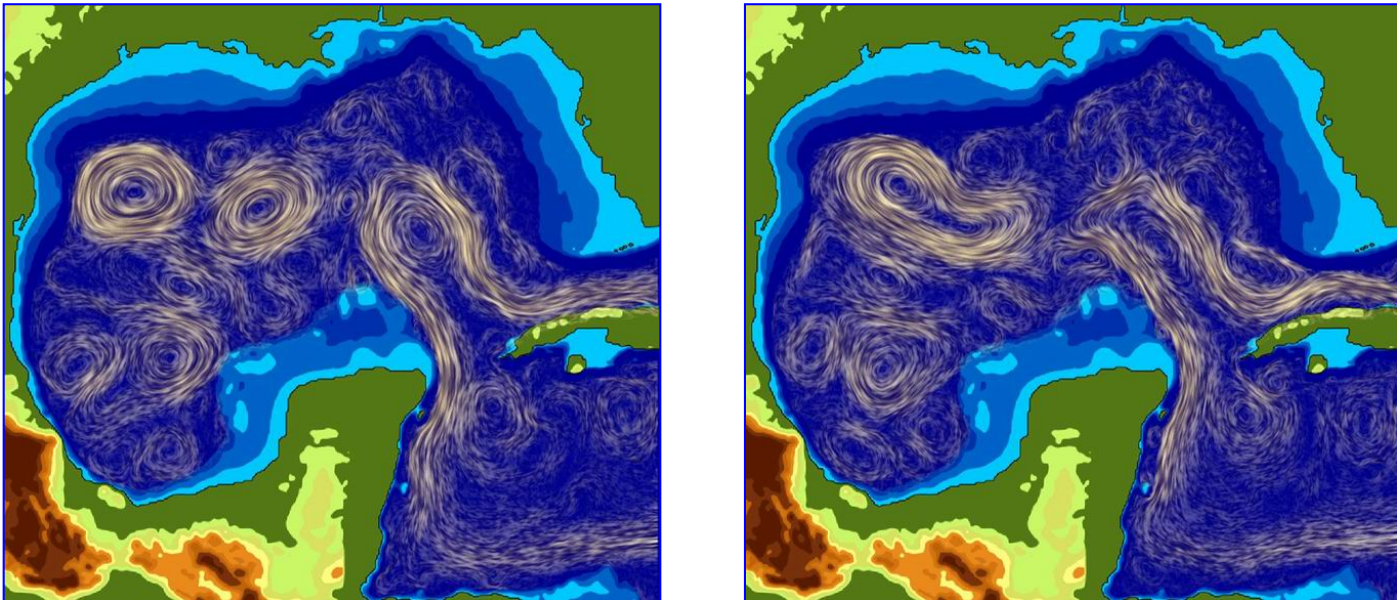
- ✧ One of the most versatile and the easiest-to-implement hardware-based methods (by *Jarke J. van Wijk, SIGGRAPH02*).
- ✧ **Basic idea:** Designs a sequence of *temporally-spatially low-pass filtered* noise textures and cyclically blends them with an iteratively advected (using *forward single-step pathline integration*) image (which is initially a BLACK rectangle).
- ✧ **Pro:** Interactive frame rates and easy simulation of many visualization techniques; good temporal coherence .
- ✧ **Con:** insufficient spatial coherence (*noisy or blurred*).



Overview — Texture-Based Methods

➤ Lagrangian-Eulerian Advection (LEA)

- ✧ A fast hardware-independent unsteady flow visualization method (by *Bruno Jobard and et al, IEEE TVCG 02*).
- ✧ **Basic idea:** Employs *backward single-step pathline integration* to **search the previous frame for the contributing particle (Eulerian)** which **scatters the texture value to the target pixel of the current frame (Lagrangian)** & blends successive textures.
- ✧ **Pro:** Interactive frame rates and supportive of arbitrarily-shaped field domains; good temporal coherence .
- ✧ **Con:** insufficient spatial coherence (obscure direction).

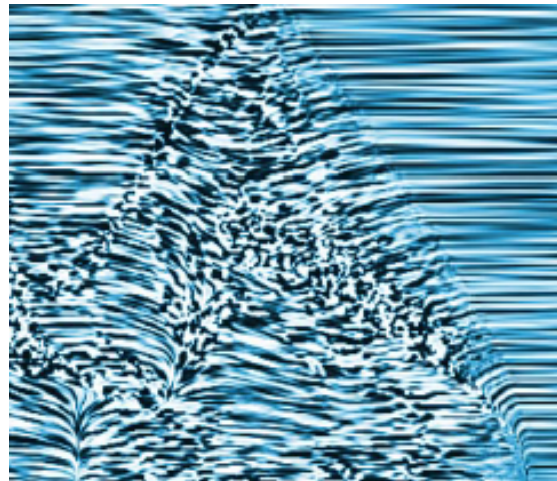
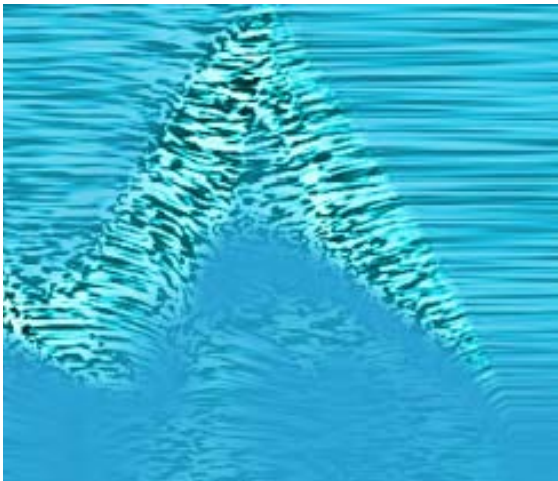


(Bruno Jobard, Gordon Erlebacher, and M. Yousuff Hussaini)

Overview — Texture-Based Methods

➤ Unsteady Flow Advection-Convolution (UFAC)

- ✧ A separable temporal-spatial texture synthesis method for unsteady flow fields (by Daniel Weiskopf and et al, *IEEE Visualization 03*).
- ✧ **Basic idea:** Establishes temporal coherence by *property advection along pathlines* while building spatial correlation by *texture convolution along streamlines*.
- ✧ With explicit, direct, and separate control over temporal coherence and spatial coherence to balance visualization speed and quality.
- ✧ **Pro:** Interactive rates on graphics cards with fragment (e.g., pixel shader) support.
- ✧ **Con:** Temporal-spatial inconsistency — either flickering animation or noisy image.



Noisy images with (left) / without (right) velocity masking

Good frames in a flickering animation

(Daniel Weiskopf, Gordon Erlebacher, and Thomas Ertl)

Overview — Texture-Based Methods

➤ Steady Flow Visualization Methods

Method	Noise design	Implementation	Image quality	Feature missing	Extensions	Performance
Spot Noise	tricky	tedious	low	yes	few	low
LIC	easy	easy	high	no	many	low

➤ Unsteady Flow Visualization Methods

Method	Temporal coherence	Spatial coherence	Performance	Graphics cards
UFLIC	high	high	low	not required
HATA	good	poor (very noisy)	near-interactive rates	special-purpose
IBFV	good	insufficient (noisy / blurred)	interactive rates	general-purpose
LEA	good	insufficient (obscure direction)	interactive	not required
UFAC	trade-off between noisy image & flickering animation		interactive	special-purpose

Recent Advances

Robert S. Laramee, Helwig Hauser, Helmut Doleisch, Benjamin Vrolijk, Frits H. Post, and Daniel Weiskopf. **The state of the art in flow visualization: dense and texture-Based techniques.** in *Computer Graphics Forum (CGF)*, Vol. 23, No. 2, 2004, pages 203-221.

Guo-Shi Li, Xavier Tricoche, Daniel Weiskopf, and Charles Hansen. Flow Charts: **Visualization of vector fields on arbitrary surface.** IEEE Transactions on Visualization and Computer Graphics, 14(5), pp. 1067-1080, 2008.

Jin Huang, Wenjie Pei, Chunfeng Wen, Guoning Chen, Wei Chen, and Hujun Bao. **Output-coherent image-space LIC for surface flow visualization.** IEEE Pacific Visualization Symposium 2012.

Jin Huang, Zherong Pan, Guoning Chen, Wei Chen, and Hujun Bao. **Image-space texture-based output-coherent surface flow visualization,** IEEE Transactions on Visualization and Computer Graphics, Vol. 19 (9): pp. 1476-1487, 2013.

Victor Matvienko, Jens Krüger. **Dense flow visualization using wave interference.** IEEE Pacific Visualization Symposium 2012.

Victor Matvienko, Jens Krüger. **Explicit frequency control for high-quality texture-based flow,** IEEE Visualization 2015.

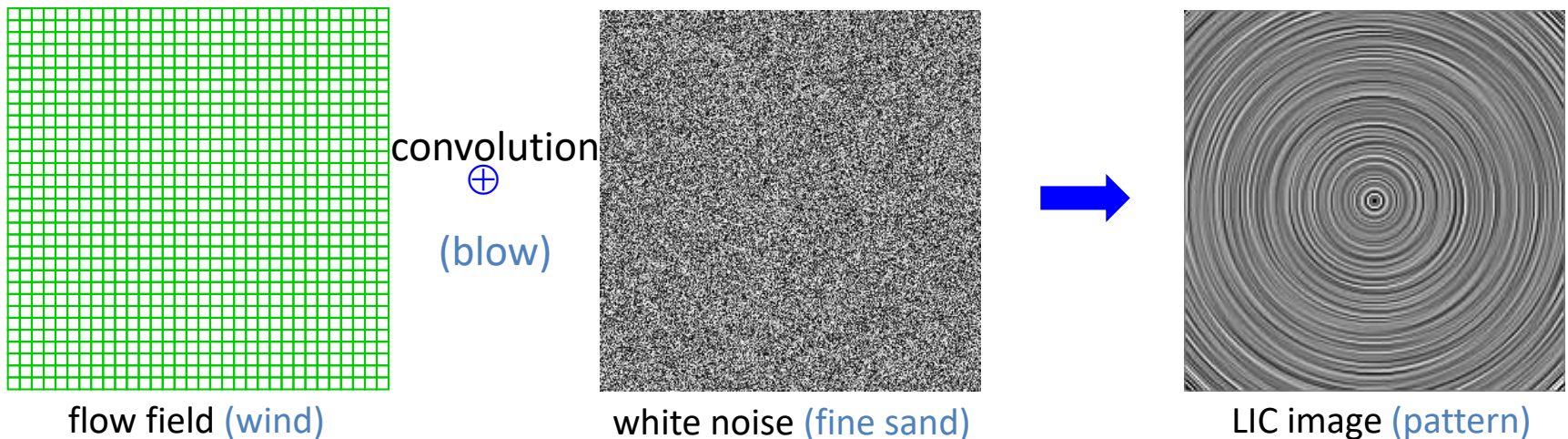
SOME DETAILS

Line Integral Convolution — LIC

Line Integral Convolution (LIC) was presented by *Brian Cabral* and *Casey Leedom* (*ACM SIGGRAPH93*). (cited by 1788 so far)

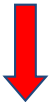
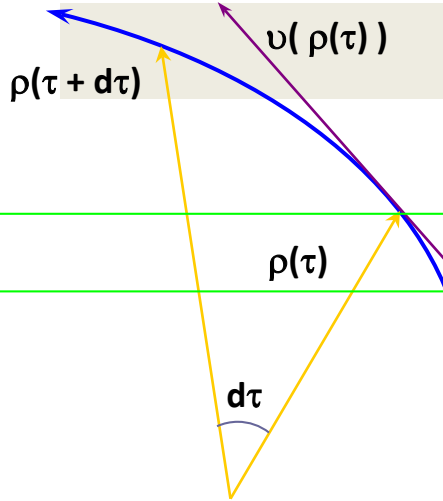
➤ Basic Idea

- ✧ LIC convolves *white noise* using a *low-pass filter* along *pixel-centered symmetrically bi-directional streamlines* to exploit spatial correlation in the flow direction — **anisotropic low-pass filtering along flow lines**.
- ✧ LIC synthesizes an image that provides a *global dense representation* of the flow, analogous to *the resulting pattern of wind-blown sand*.



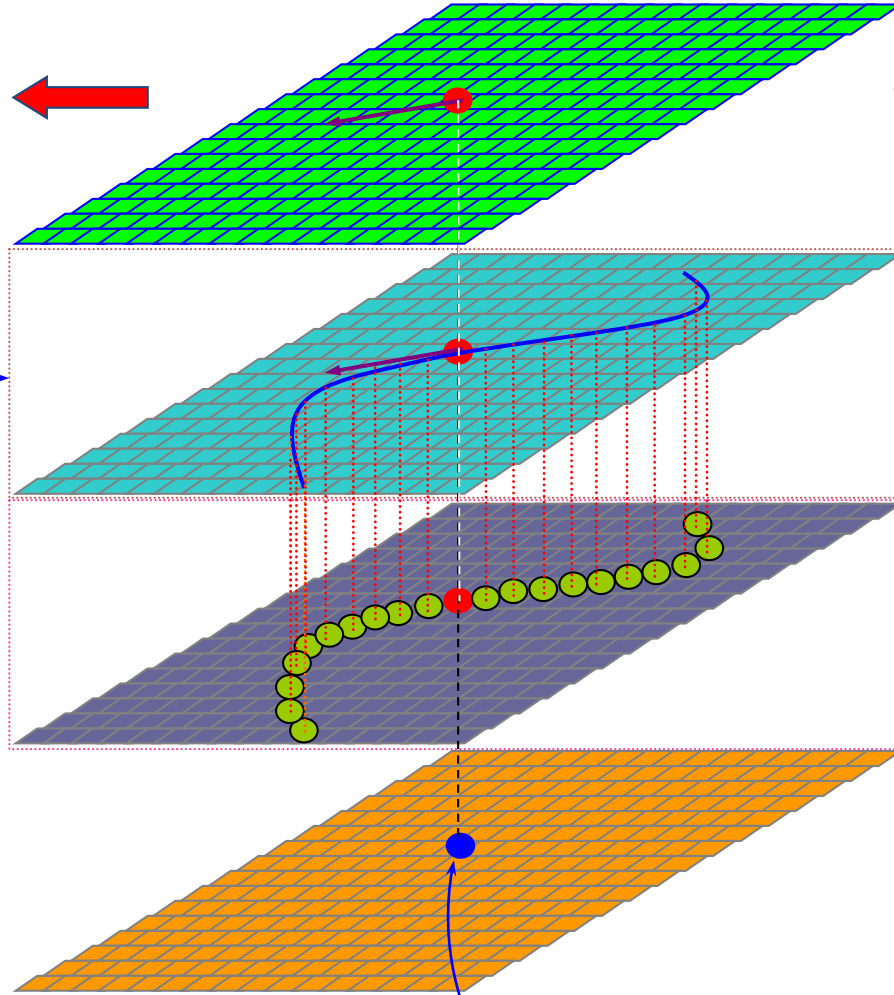
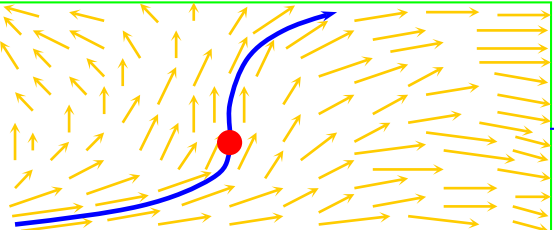
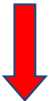
white noise → the texture is freely warped / driven by the flow without any intrinsic resistance

Line Integral Convolution — LIC



$$\frac{d(\rho(\tau))}{d\tau} = v(\rho(\tau))$$

$$\rho(\tau + \Delta\tau) = \rho(\tau) + \int_{\tau}^{\tau + \Delta\tau} v(\rho(\tau)) d\tau$$



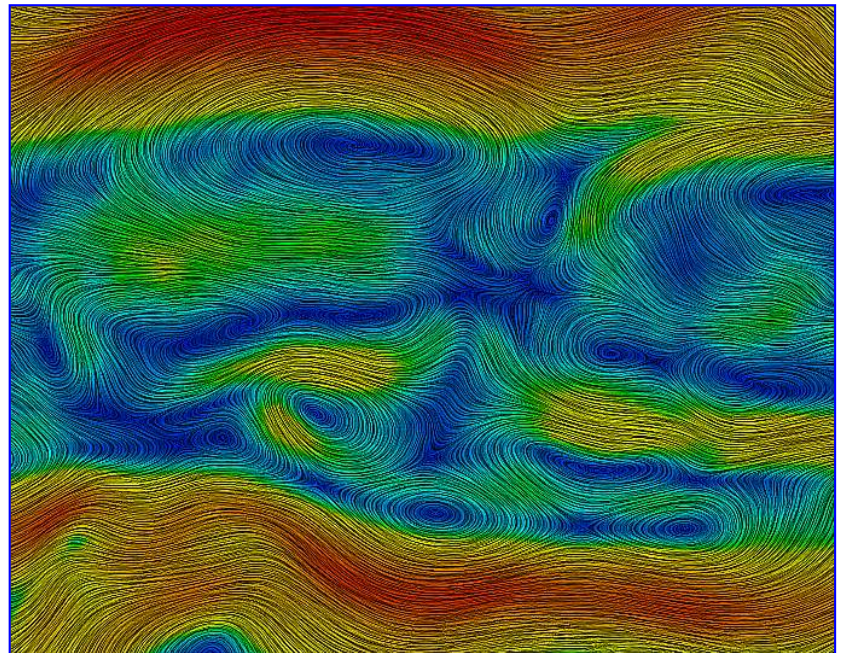
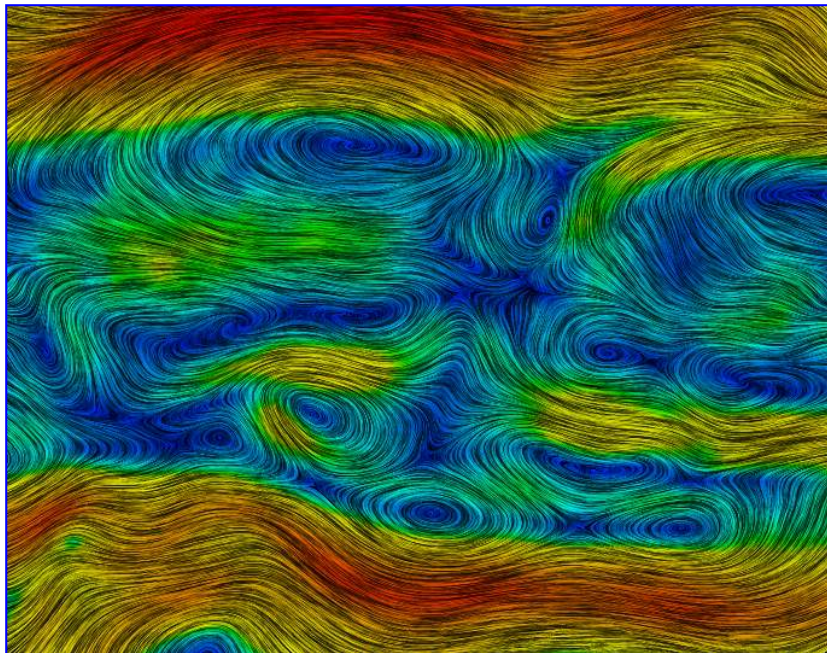
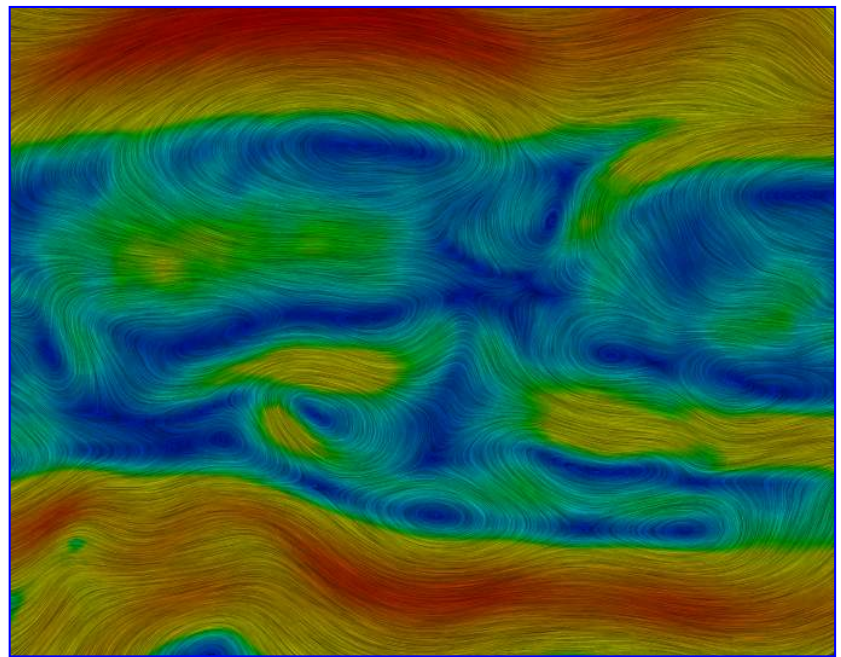
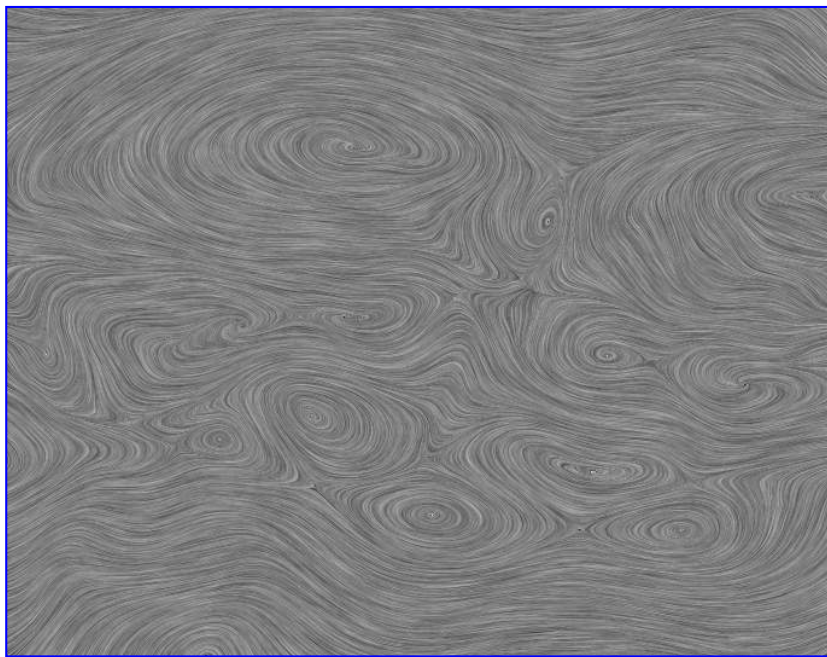
a point in the flow field, the counterpart of a pixel in the output LIC image

the correlated pixels along the streamline

index the input noise for the texture values

compute the target pixel value in the LIC image by convolution

$$T'(\rho(0)) = \frac{\int_{-L}^L K(\tau) T(\rho(\tau)) d\tau}{\int_{-L}^L K(\tau) d\tau}$$

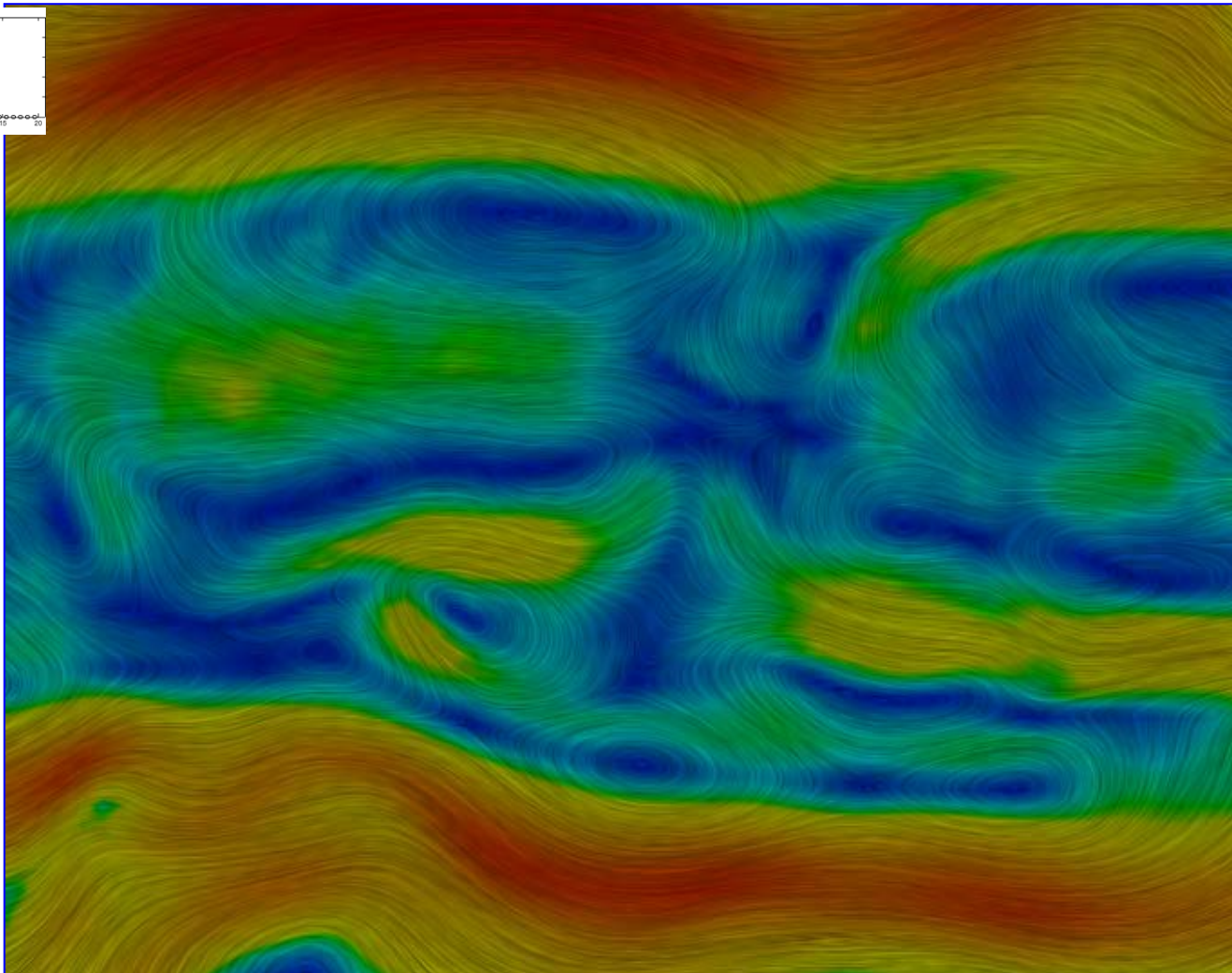
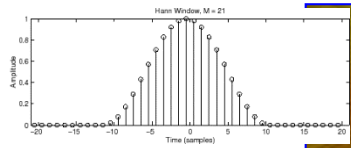


Top-left: gray-scale LIC
Bottom-left: contrasted LIC

Top-right: color-mapped LIC
Bottom-right: high-pass filtered LIC

Line Integral Convolution — LIC variant

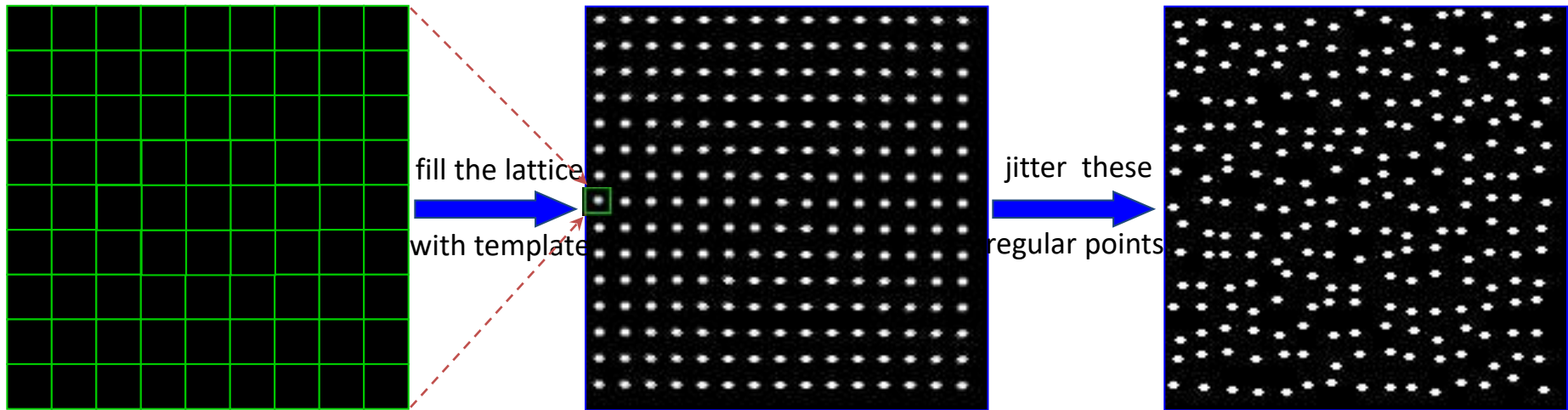
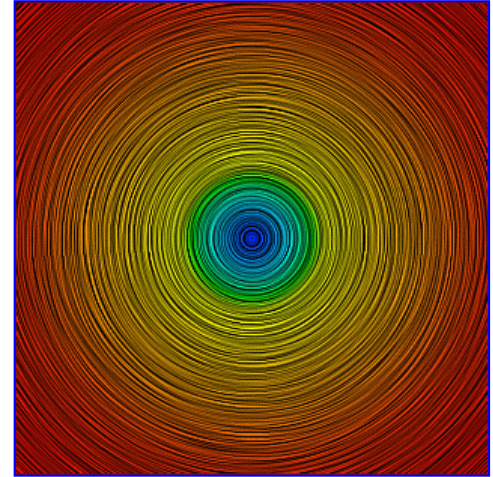
- **Animation** successively shifting the phase of a periodic convolution kernel such as Hanning filter (“Motion Without Movement”, CG ’91)



Line Integral Convolution — LIC Variants

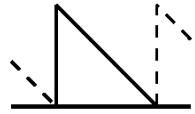
➤ OLIC (Oriented LIC)

- ✧ R. Wegenkittl and et al. (*Computer Animation 97*).
- ✧ A LIC image shows the flow **direction** while failing to show the **orientation** (clockwise or counter-clockwise?).
- ✧ A ramp filter offers orientation cue by *intensity tapering*.
- ✧ *Sparse noise* offers *enough space for intensity-tapering*.
- ✧ White points of some size are placed at the lattice and then *slightly jittered*.

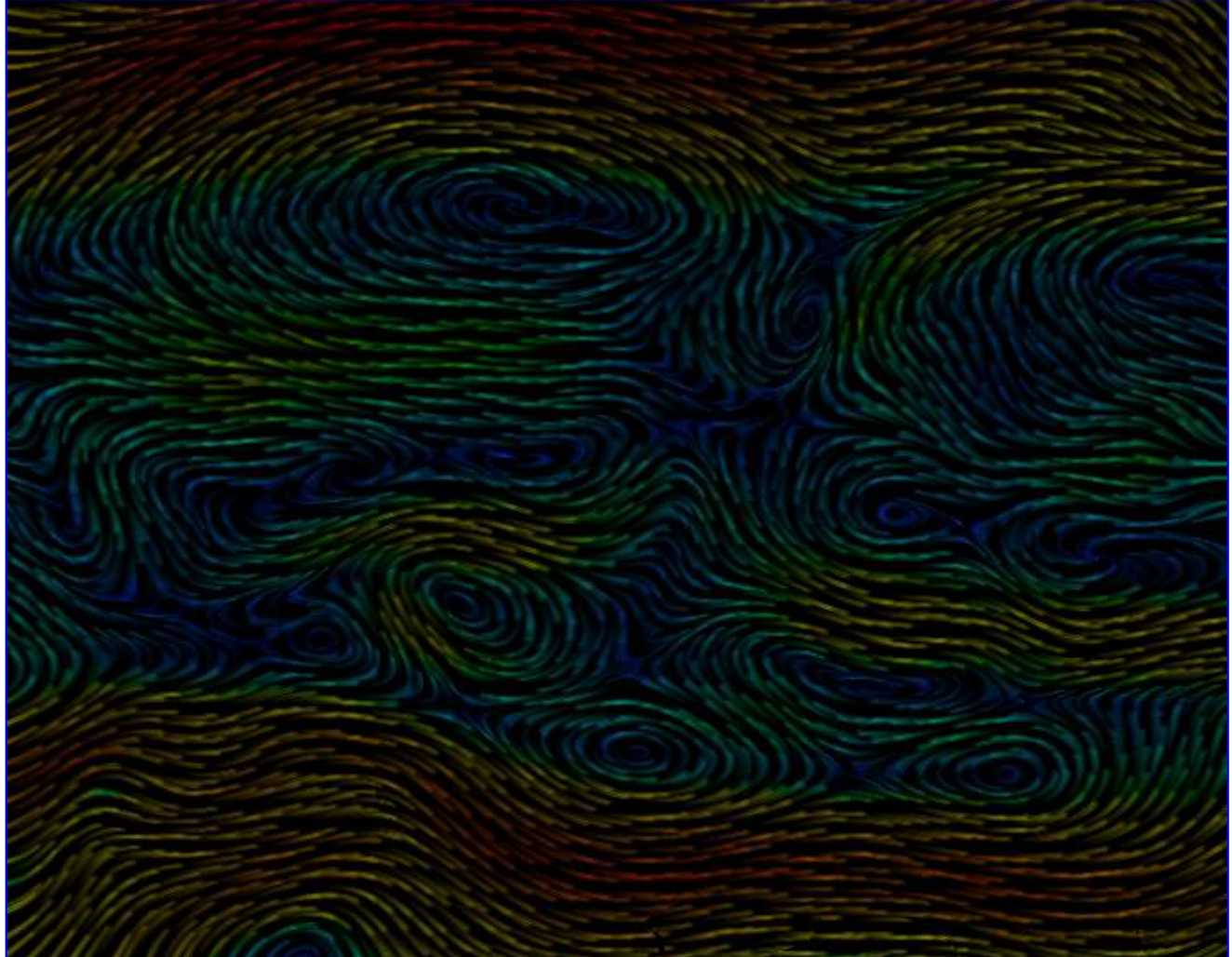
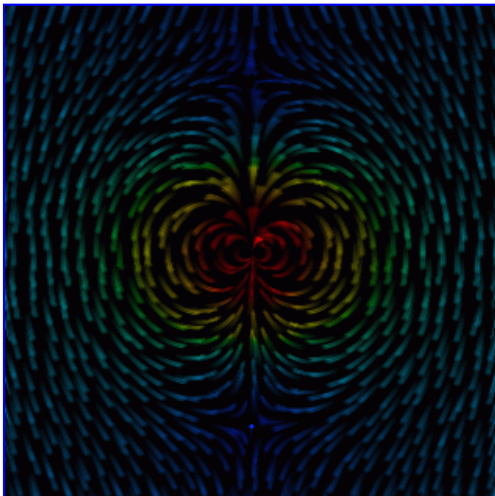
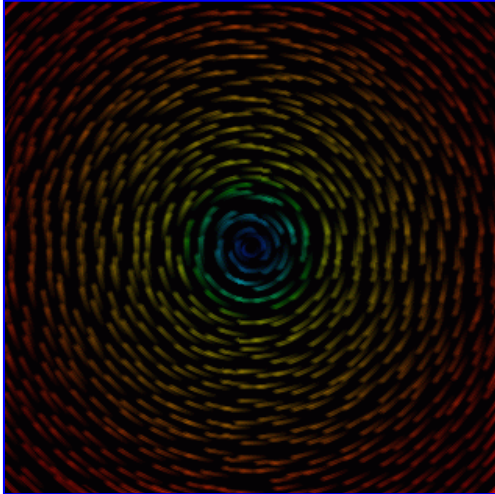


the design of sparse noise

Line Integral Convolution — LIC Variants



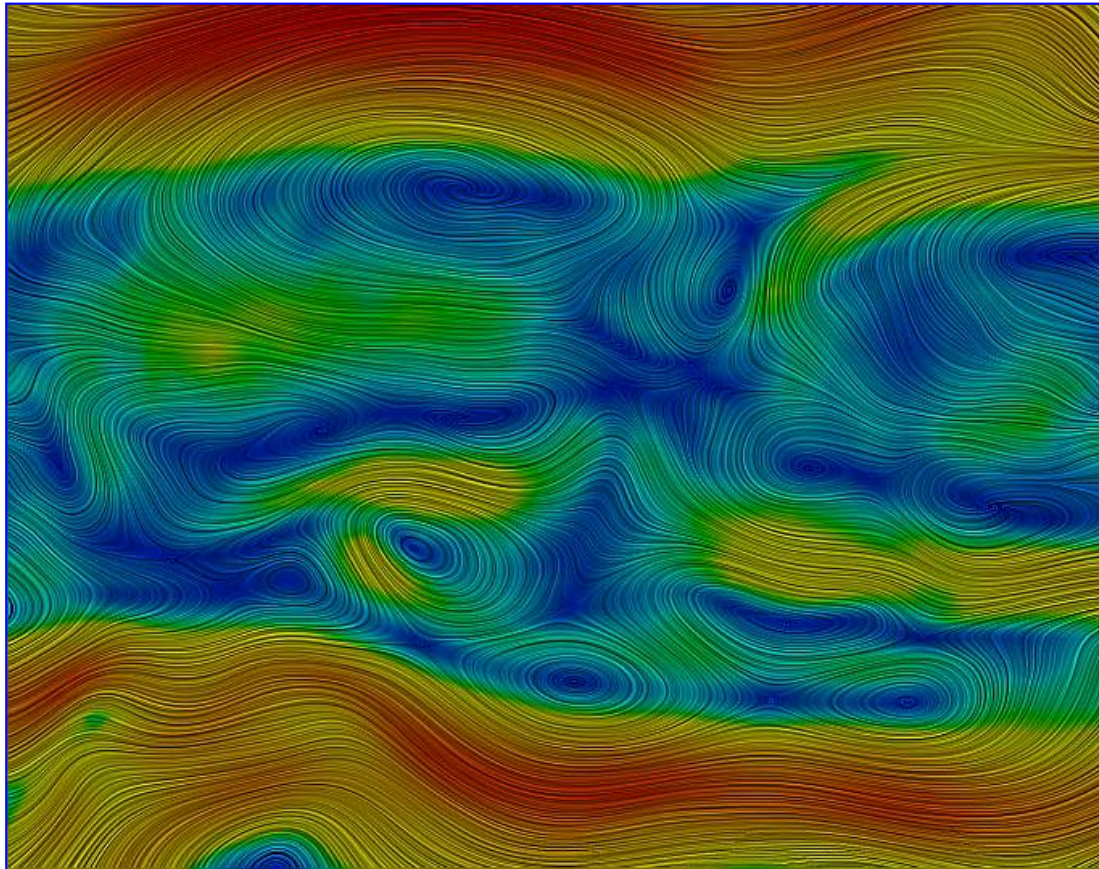
Sparse noise \oplus Ramp convolution kernel \Rightarrow OLIC (flow orientation in a LIC image)



Line Integral Convolution — LIC Variants

➤ Enhanced LIC

- ✧ A. Okada and D. L. Kao (*IS & T / SPIE Electronics Imaging 97*).
- ✧ *Enhances the appearance of streamlines* — neither noisy nor blurred.
- ✧ Iteratively (iteration times ≥ 2) *takes an output LIC image as the input to the next LIC cycle prior to final high-pass filtering* (e.g., Laplacian filter).



Line Integral Convolution — LIC Variants

A quite fancy LIC image results from using *sparse noise* in enhanced LIC.

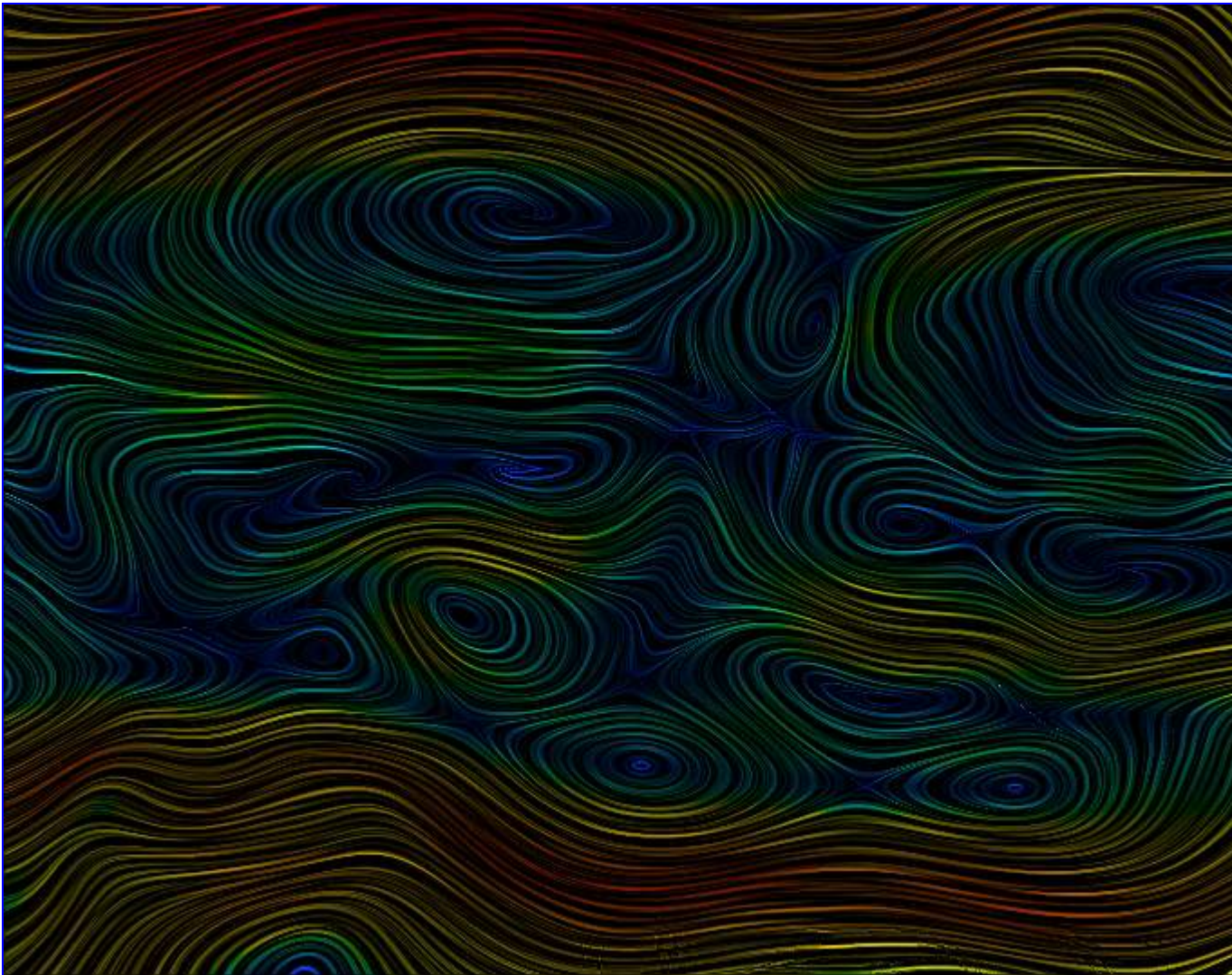
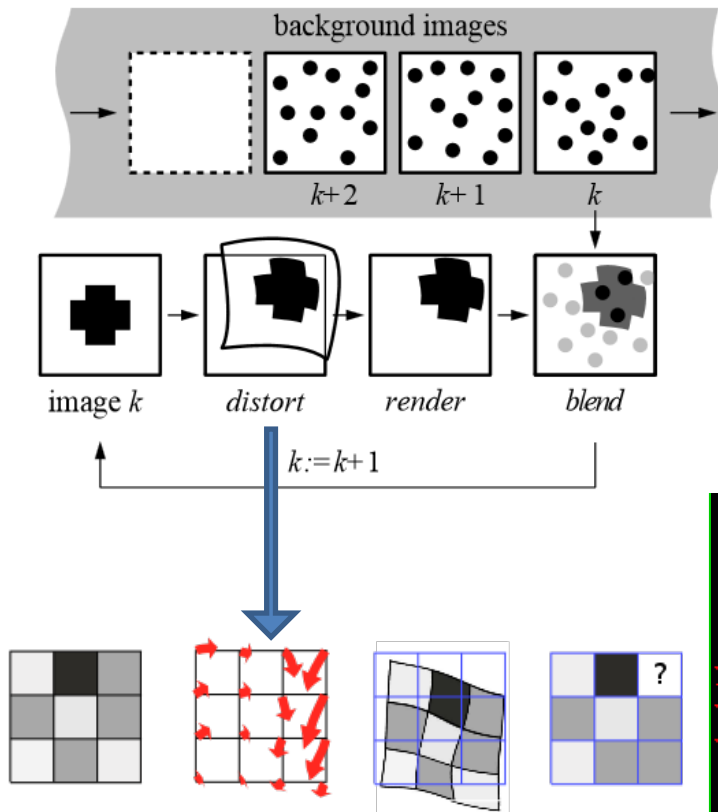


IMAGE-BASED FLOW VISUALIZATION (IBFV)

Details — Texture-Based Methods

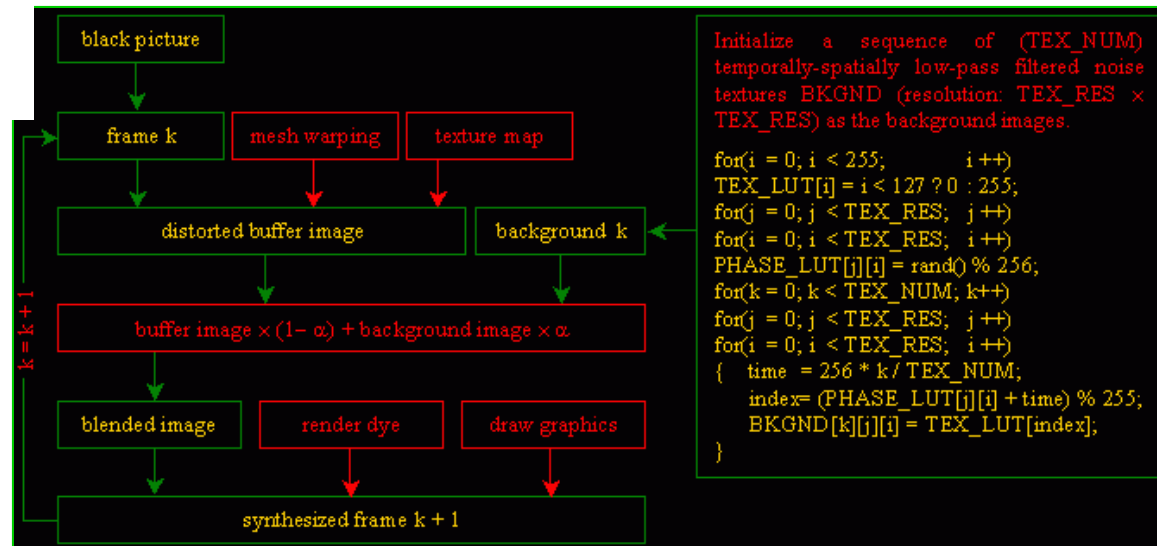
➤ Image-Based Flow Visualization (IBFV)

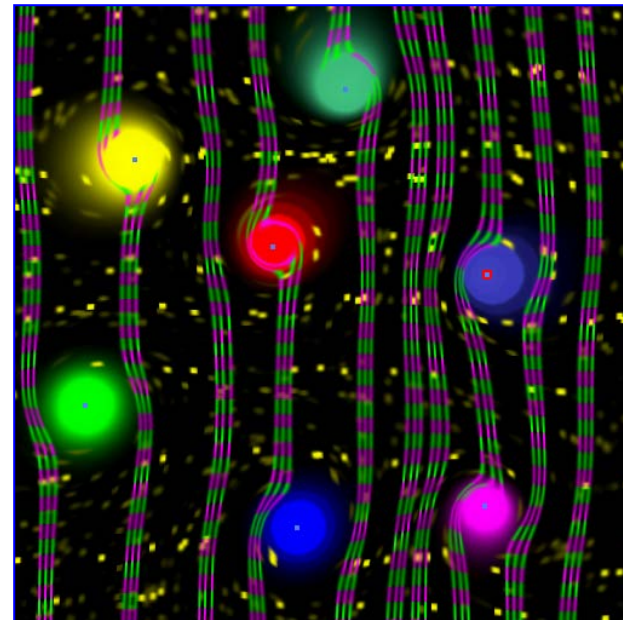
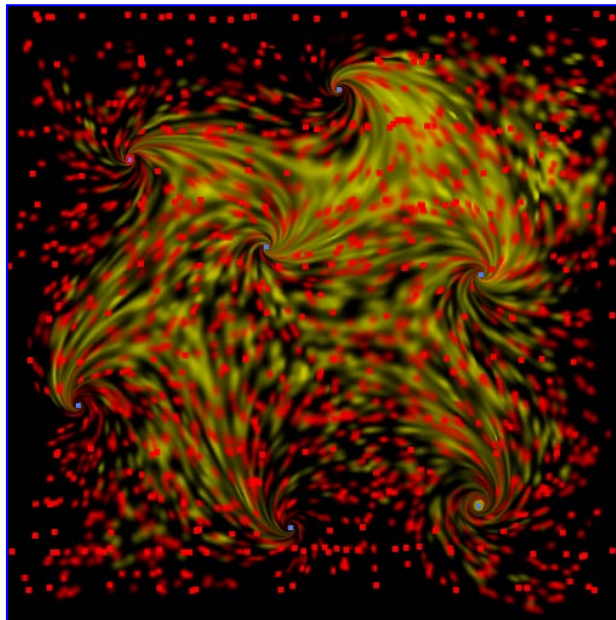
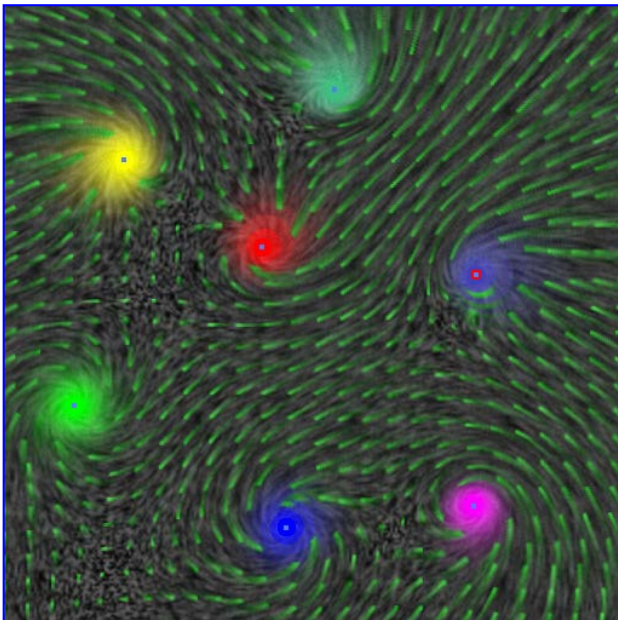
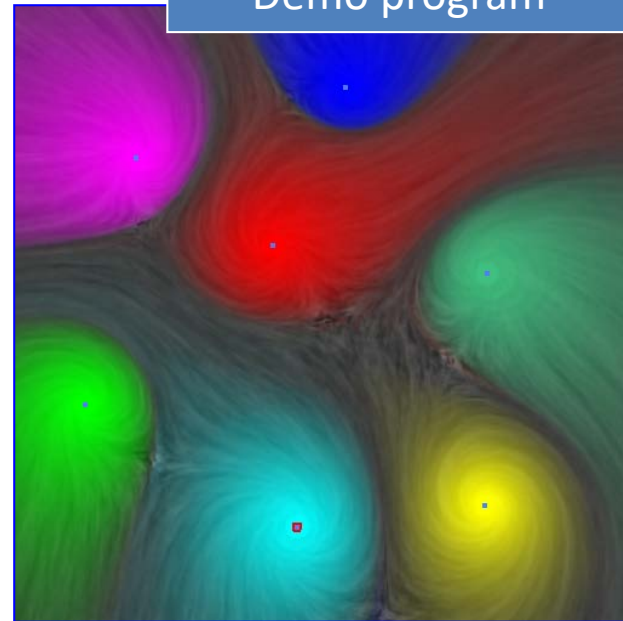
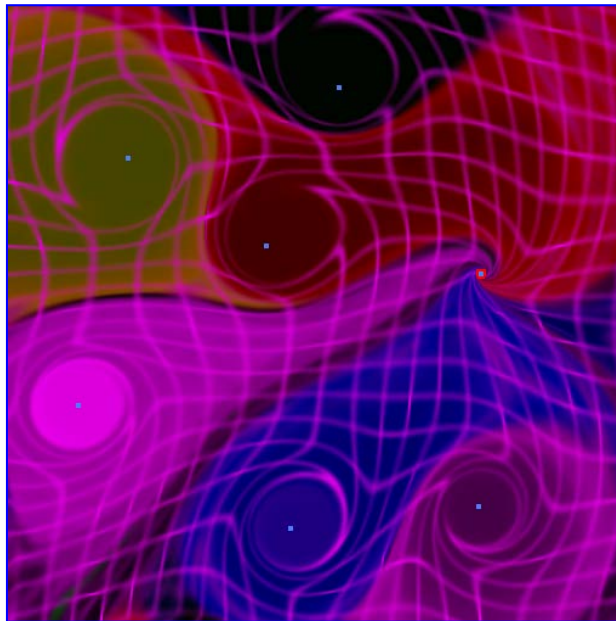
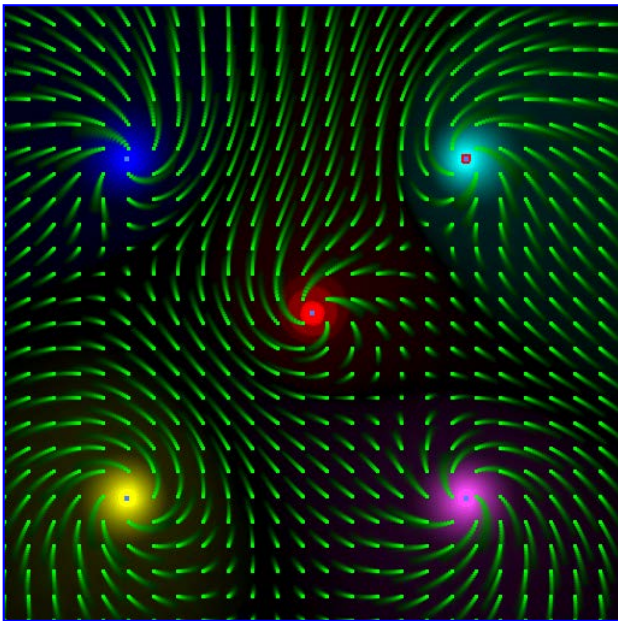


$$F(\mathbf{p}_k; k) = (1 - \alpha)F(\mathbf{p}_{k-1}; k - 1) + \alpha G(\mathbf{p}_k; k)$$



$$F(\mathbf{p}_k; k) = \alpha \sum_{i=0}^{k-1} (1 - \alpha)^i G(\mathbf{p}_{k-i}; k - i)$$





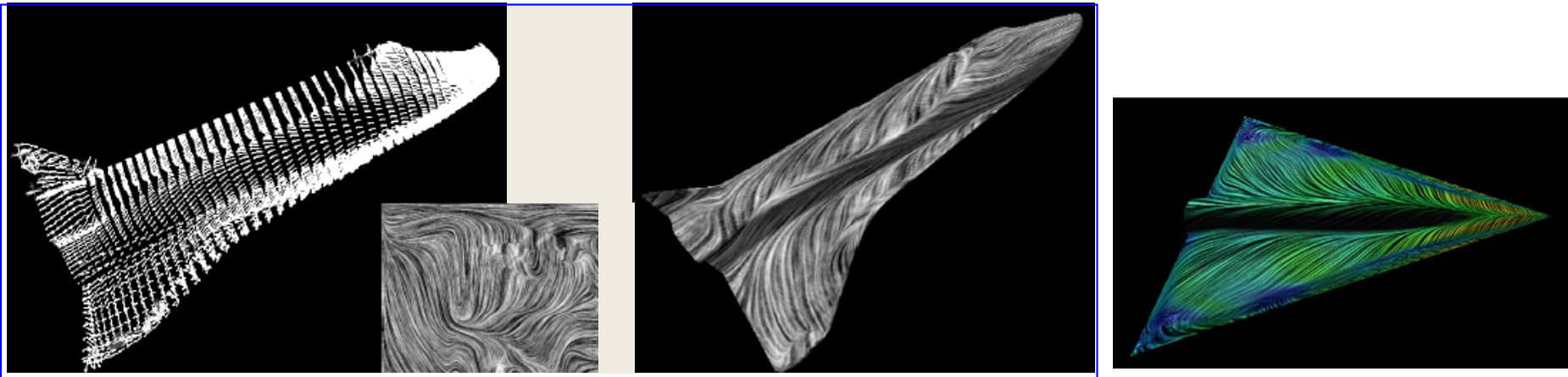
A variety of visualization techniques such as particles, arrow plots, streamlines, timelines, spot noise, LIC, and flow topology can be easily simulated by tuning IBFV parameters

TEXTURE-BASED VISUALIZATION FOR SURFACE FLOW

Line Integral Convolution — LIC Variants

➤ Surface LIC

- ✧ Dense visualization of flows on curved surfaces
- ✧ **Parametric surface LIC — on well-defined surfaces**
 - ◆ On a parameterized CFD surface (model).
 - ◆ On a parameterized stream surface extracted by *Advancing Front* from 3D flows.
 - ◆ *Maps vectors from physical space to parametric space by nonlinear transform.*
 - ◆ *Generates a 2D LIC texture in parametric space.*
 - ◆ *Maps the 2D LIC texture back onto the curved surface (physical space).*
 - ◆ Compensates **texture distortions from non-isometric physical-parametric space mapping** by using carefully-designed input noise and adaptive kernel length.

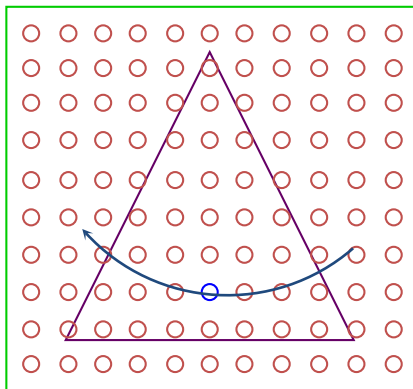


(Lisa Forssell et al., IEEE TVCG 95)

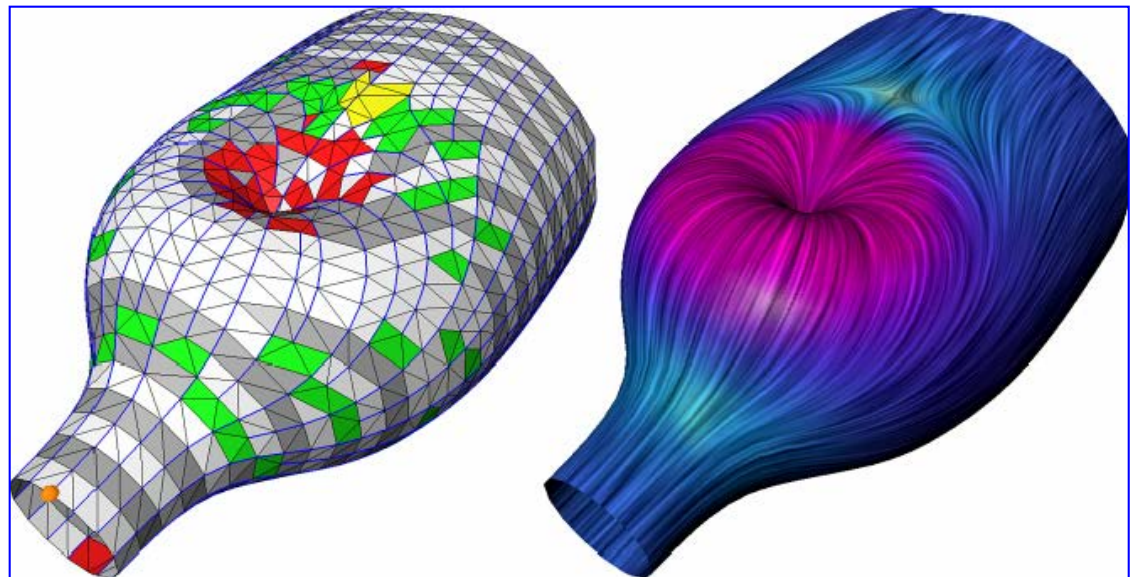
Line Integral Convolution — LIC Variants

✧ Triangulated surface LIC — on arbitrarily complex surfaces

- ◆ On extracted iso-surfaces or other implicit surfaces through a volume flow.
- ◆ Adopts fast and robust streamline integration directly on a triangular domain.
- ◆ **Obviates non-isometric space mapping to avoid texture distortions.**
- ◆ Uses *solid noise* (usually by a procedural noise function).
- ◆ Obtains the value of each **texel (texture element)** sampled in a triangle via LIC.
- ◆ Efficiently *packs numerous triangular-textures* into a few rectangular-texture blocks stored in memory for fast texture retrieval at low memory cost.
- ◆ Maps each triangular texture onto the target triangle in rendering.



compute each texel value

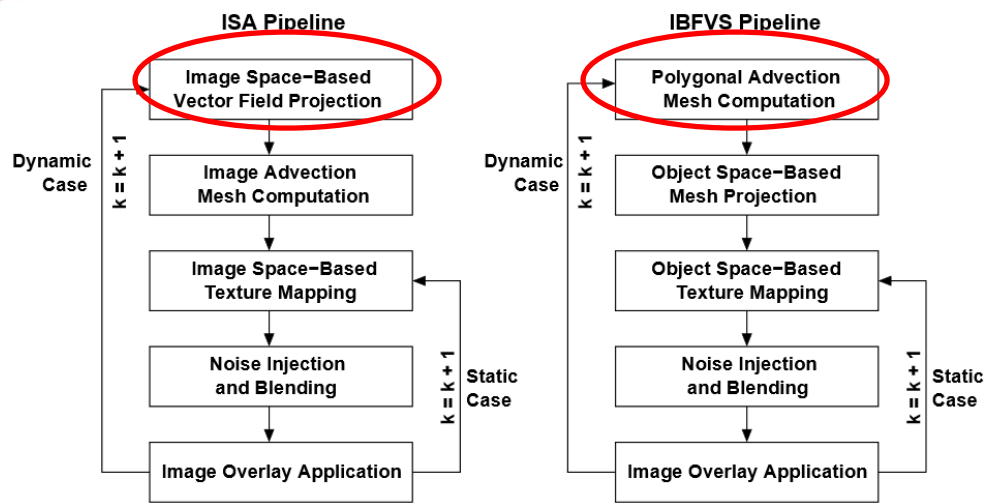
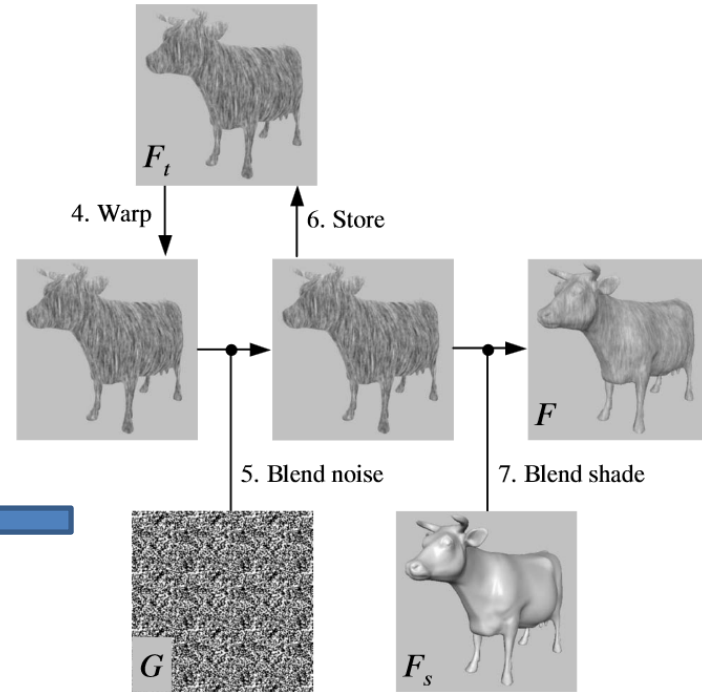
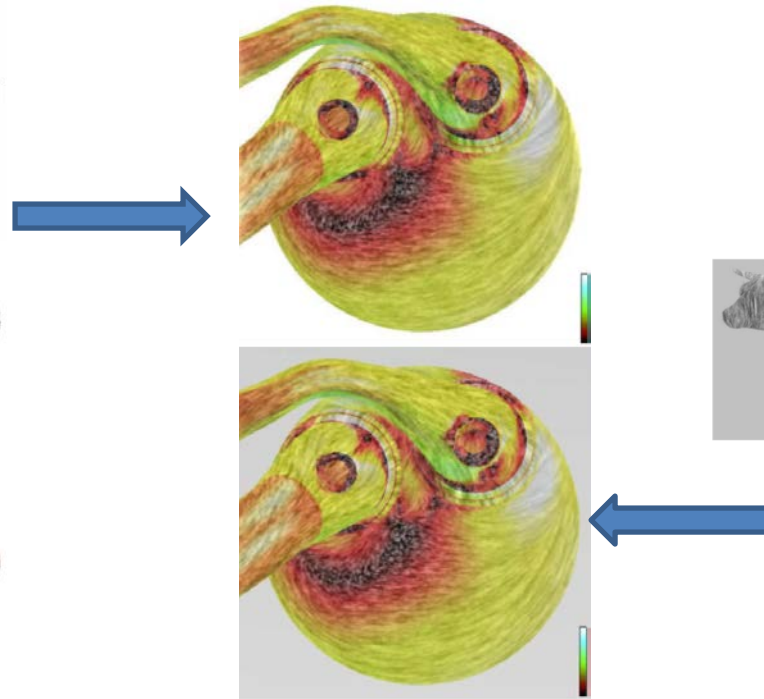


(Detlev Stalling, ZIB, Germany)

ISA vs. IBFVS

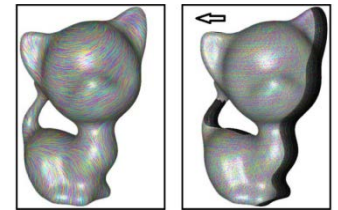
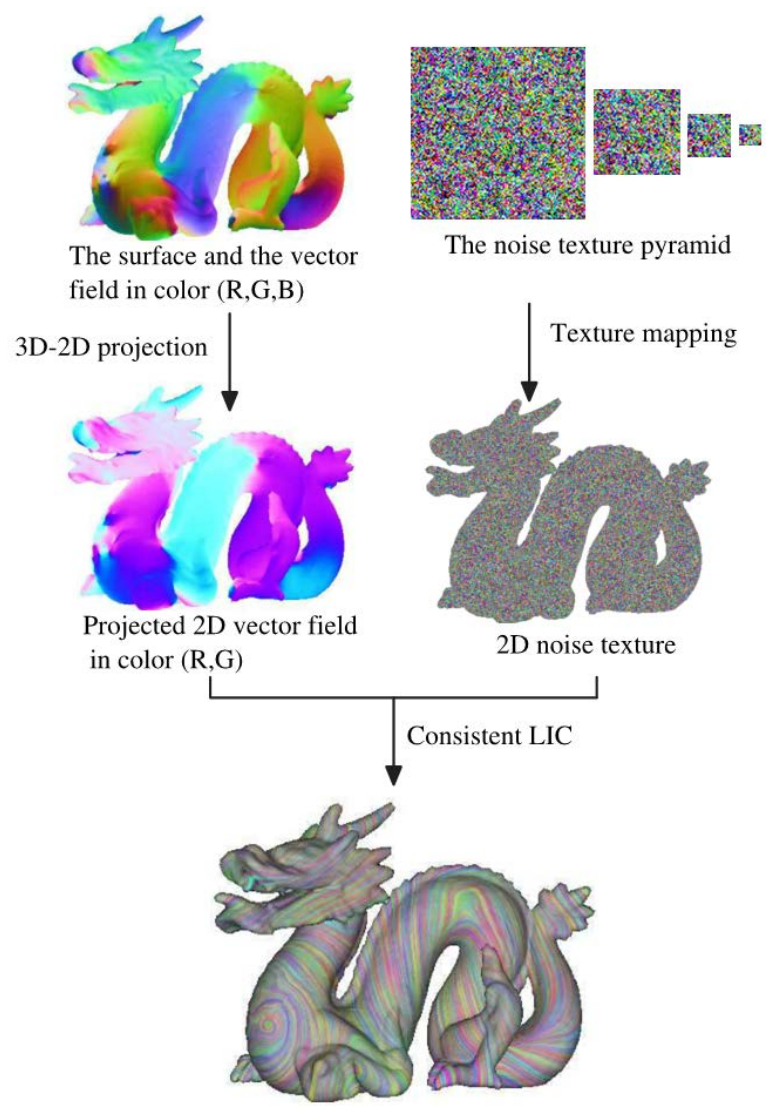


ISA

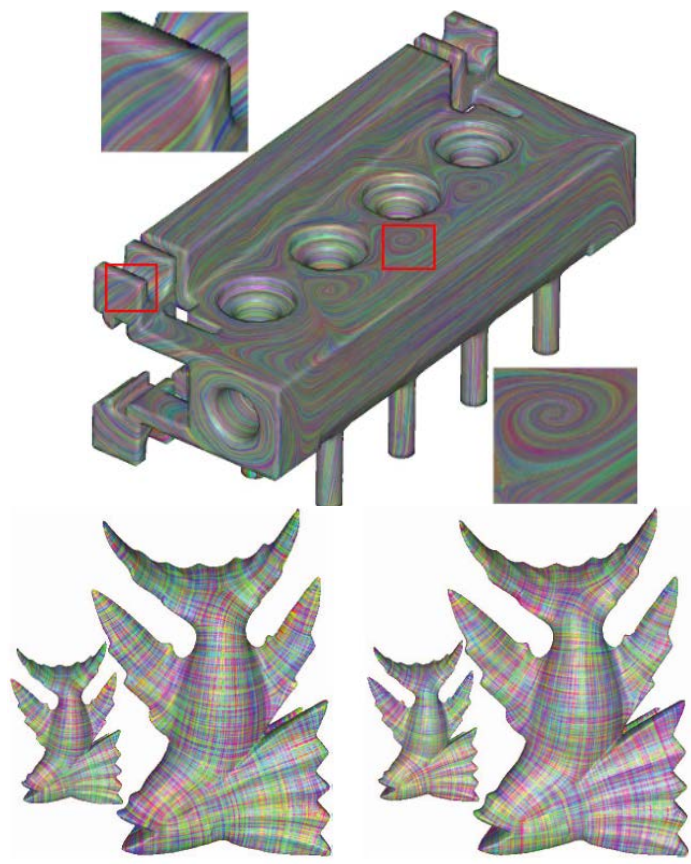


IBFVS

Coherent Texture on Surfaces



Address the inconsistency of flow image when the view point is changed.

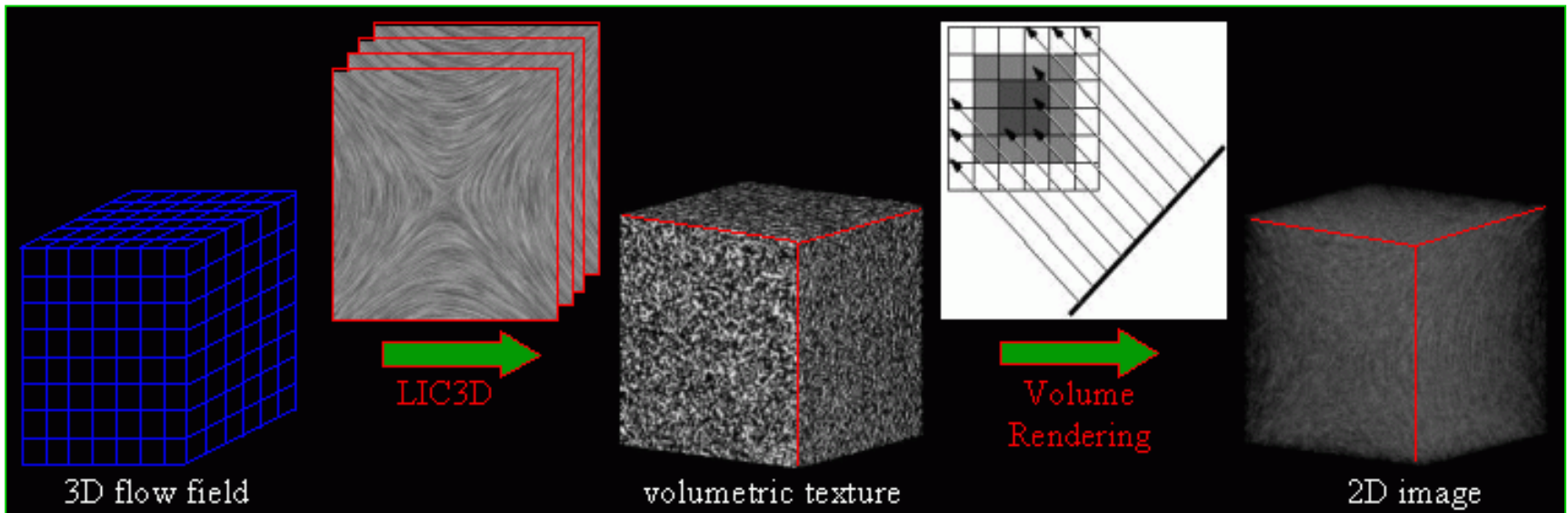


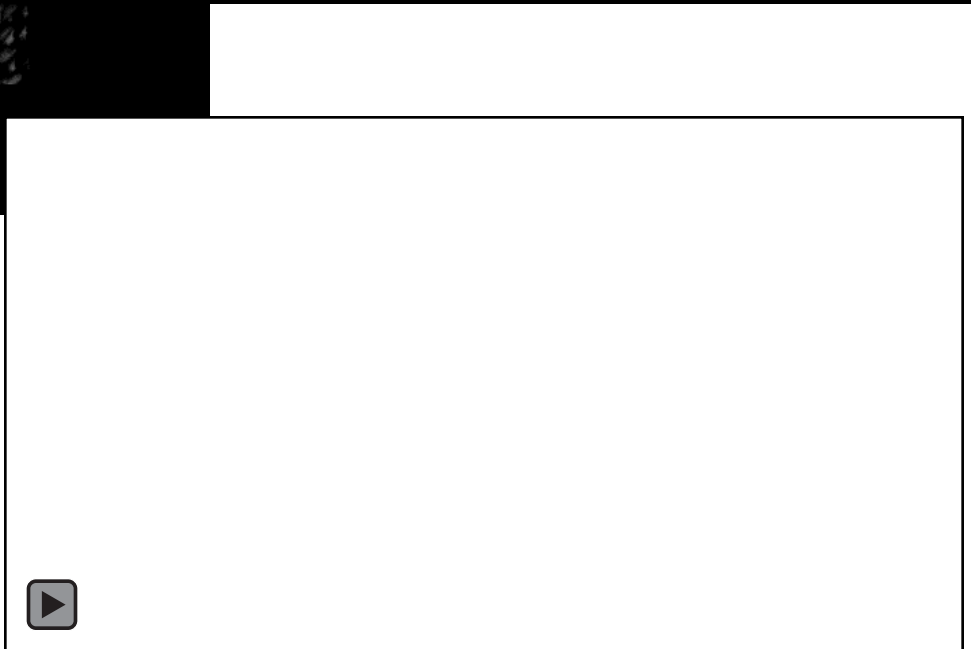
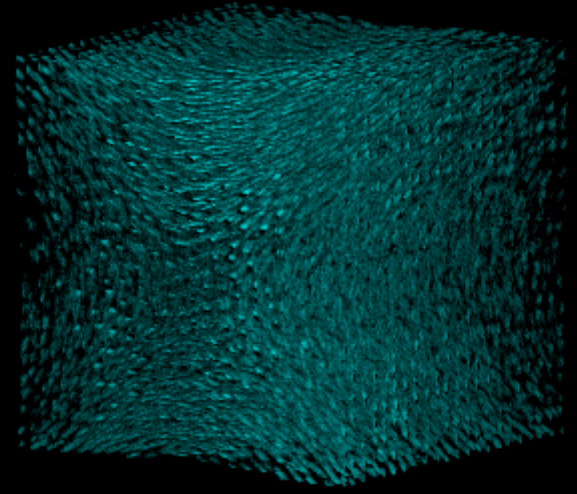
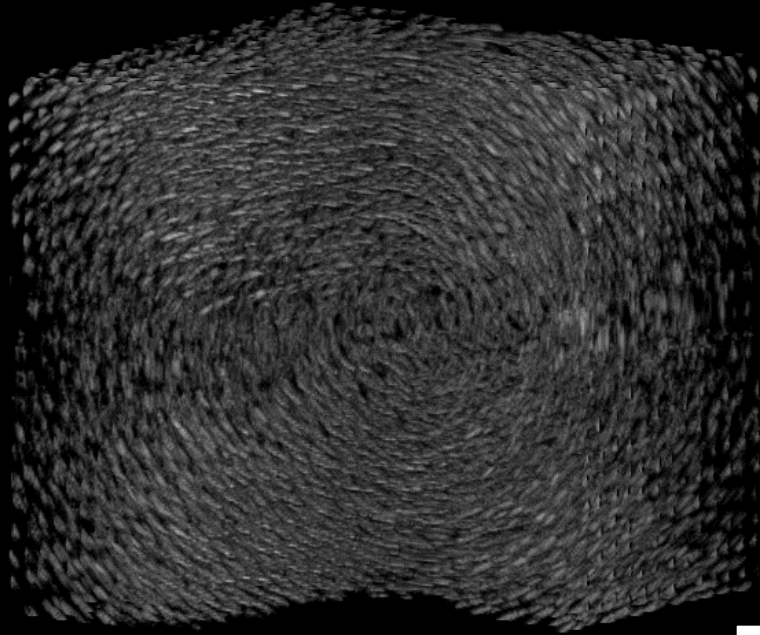
TEXTURE-BASED VISUALIZATION FOR 3D FLOW

Line Integral Convolution — LIC Variants

➤ Volume LIC

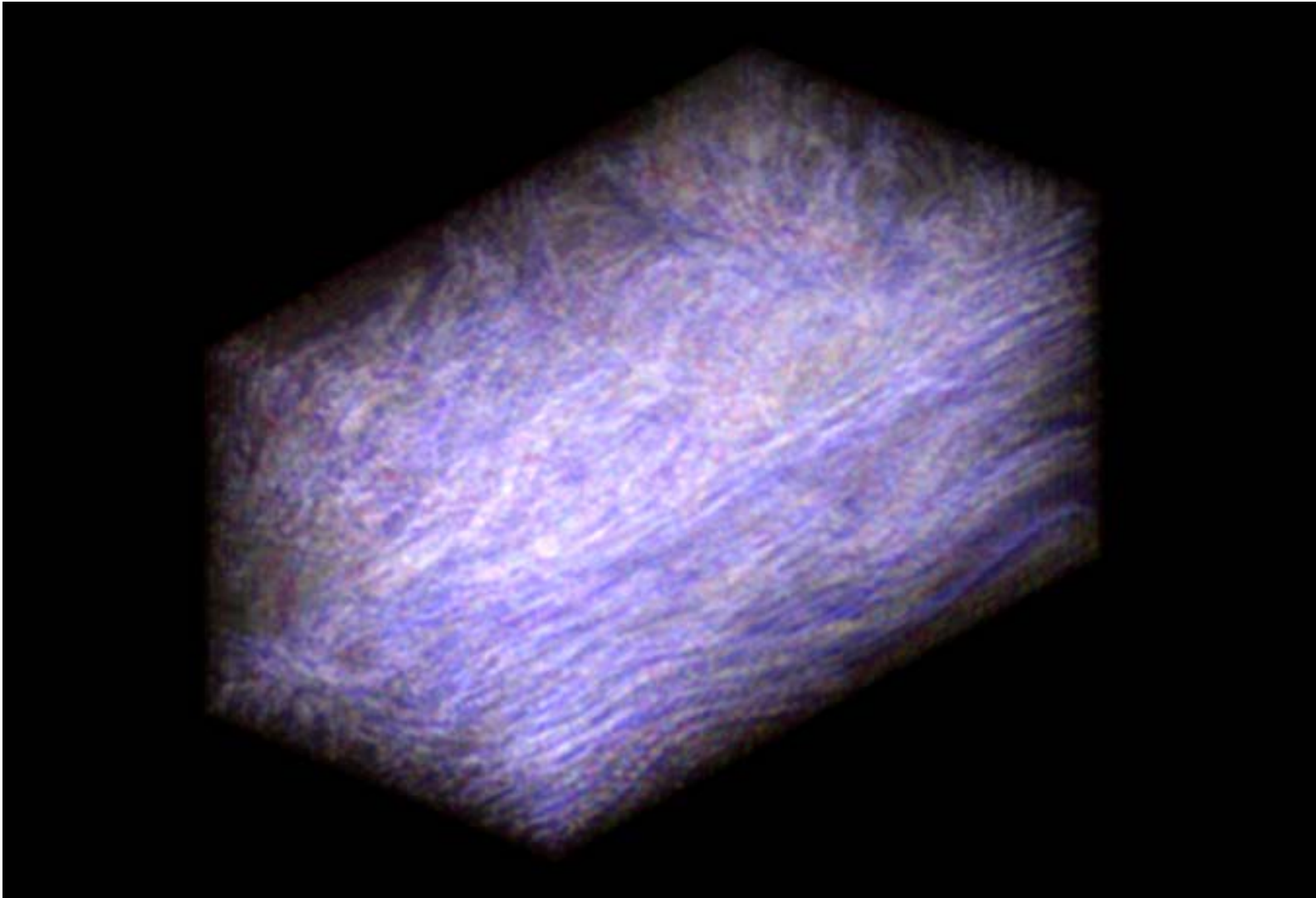
- ✧ Victoria Interrante and Chester Grosch (*IEEE Visualization 97*).
- ✧ A straightforward extension of LIC to 3D flow fields.
- ✧ Low-pass filters *volumetric noise* along 3D streamlines.
- ✧ Uses *volume rendering* to display resulting 3D LIC textures.
- ✧ Very time-consuming to generate 3D LIC textures.
- ✧ Texture values offer no useful guidance for transfer function design due to *lack of intrinsic physical info* that can be exploited to distinguish components.
- ⇒ Very challenging to clearly show *flow directions and interior structures through a dense texture volume*.

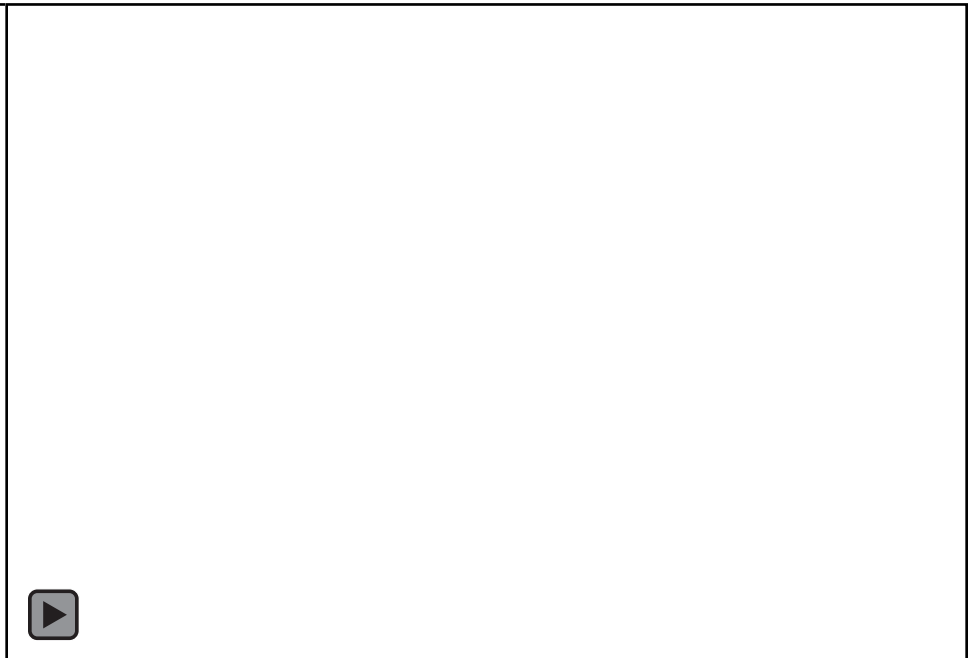
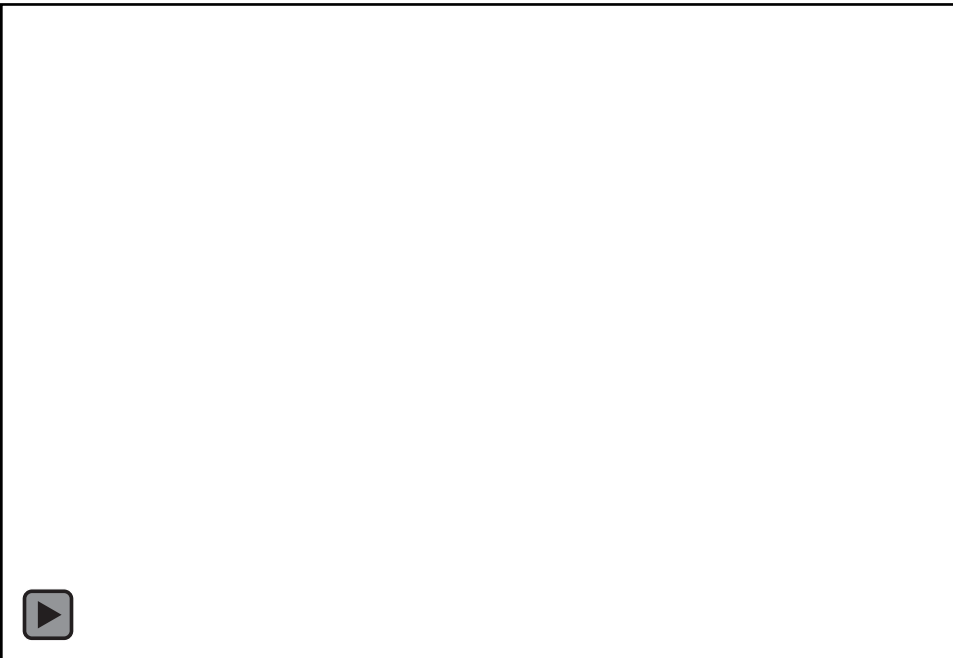
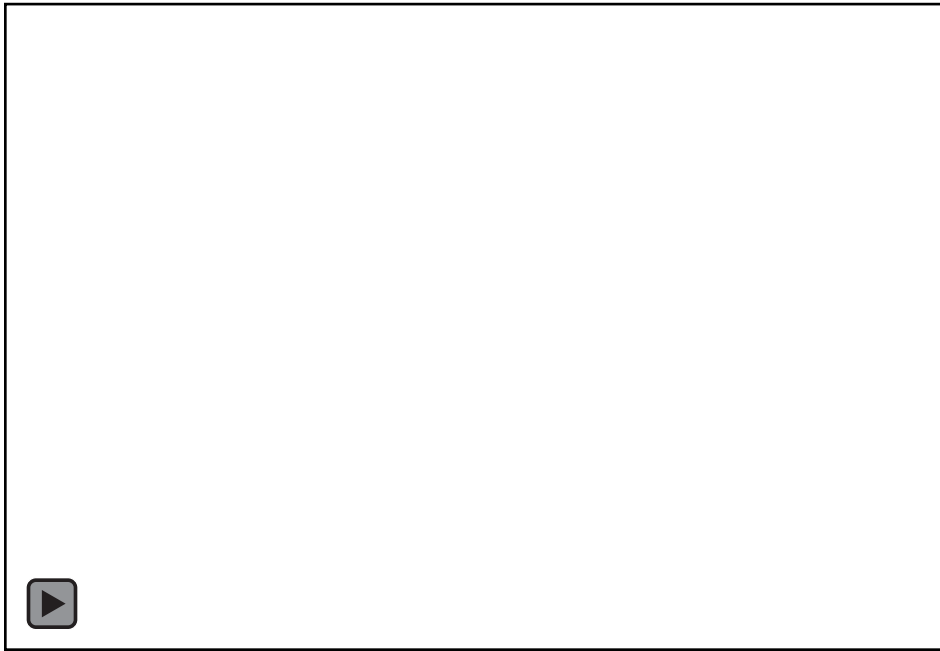




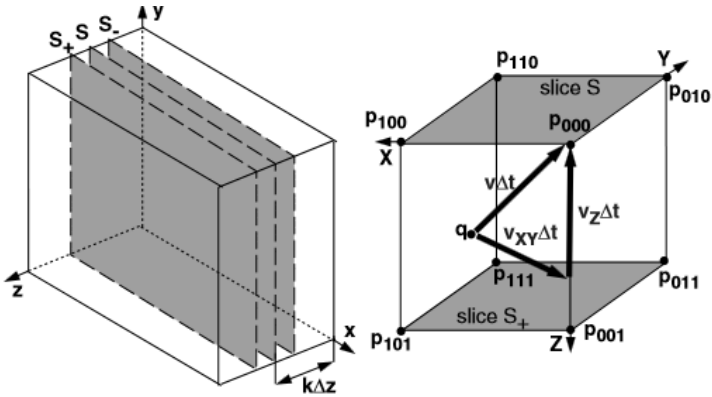
Unsteady Flow LIC — VAUFLIC

Image generated by using a texture-based transfer function





3D IBFV

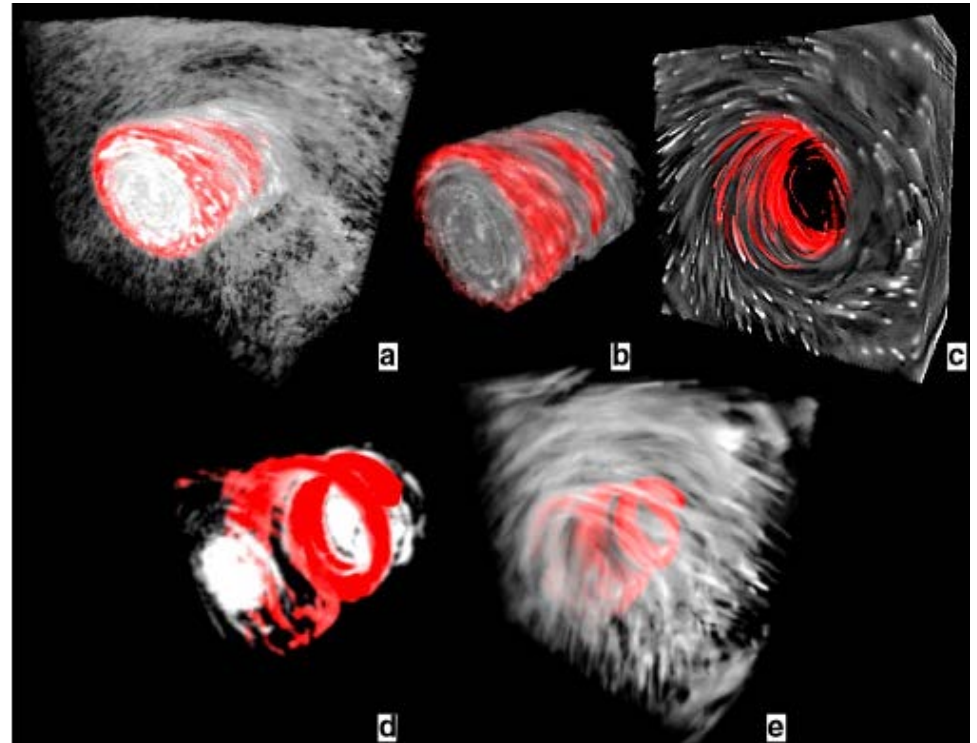
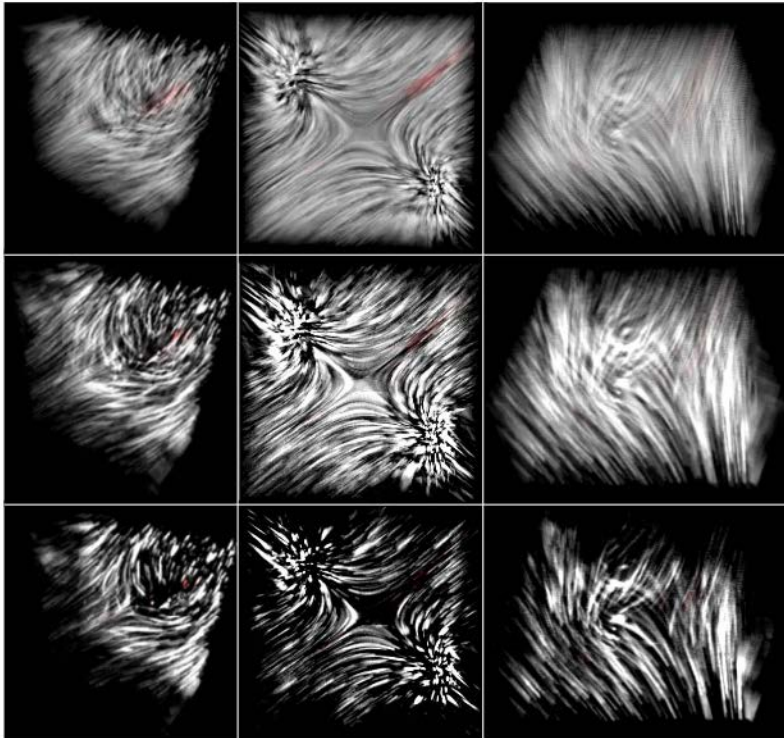


for $i = 0$ to $N-1$

- ```

{
 if ($i > 0$)
 do 1D Z-axis advection from S_{i-1} to S_i
 if ($i < N-1$)
 do 1D Z-axis advection from S_{i+1} to S_i
 do 2D IBFV-based advection in the slice S_i
}

```
- (1)
- (2)
- (3)



[Telea and van Wijk Vis03]



# Additional reading

- Helwig Hauser, Robert S. Laramée, Helmut Doleisch, Frits H. Post, and Benjamin Vrolijk, **The State of the Art in Flow Visualization: Direct, Texture-based, and Geometric Techniques**, *TR-VRVis-2002-046* Technical Report, VRVis Research Center, Vienna, Austria, December 2002.
- Robert S. Laramée, Helwig Hauser, Helmut Doleisch, Benjamin Vrolijk, Frits H. Post, and Daniel Weiskopf, **The State of the Art in Flow Visualization: Dense and Texture-Based Techniques**. in *Computer Graphics Forum (CGF)*, Vol. 23, No. 2, 2004, pages 203-221.

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