



CHAPTER VIII VIRTUAL MEMORY REVIEW QUESTIONS

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Chapter overview

- Virtual Memory
 - Address translation
 - On-demand fetch
- Page table organization
- Page replacement policies
 - Performance issues



Problem

- A computer has 32 bit addresses and a virtual memory with a page size of 8 kilobytes.
 - How many bits are used by the *byte offset*?
 - What is the size of a *page table*?



First part

- A computer has 32 bit addresses and a virtual memory with a page size of 8 kilobytes.
 - How many bits are used by the *byte offset*?



Solution

- A computer has 32 bit addresses and a virtual memory with a page size of 8 kilobytes.
 - How many bits are used by the *byte offset*?
 - 8 kilobytes = 2^{13} bytes
 - The byte offset uses 13 bits



Second part

- A computer has 32 bit addresses and a virtual memory with a page size of 8 kilobytes.
 - What is the size of a *page table*?



Solution

- A computer has 32 bit addresses and a virtual memory with a page size of 8 kilobytes.
 - What is the size of a *page table*?
 - Since the byte offset uses 13 bits, the page number will use $32 - 13 = 19$ bits
 - Page tables will have $2^{19} = 512\text{K}$ entries



Problem

- A computer system has 32-bit addresses and a page size of 4 kilobytes.
 - What is the maximum number of pages a process can have?
 - How many bits of the virtual address will remain *unchanged* during the address translation process?



First part

- A computer system has 32-bit addresses and a page size of 4 kilobytes.
 - What is the maximum number of pages a process can have?



Solution

- A computer system has 32-bit addresses and a page size of 4 kilobytes.
 - What is the maximum number of pages a program can have?
 - We divide the size of the virtual address space by the page size:

$$2^{32} \text{ B} / 4 \text{ KB} = 2^{32} / 2^{12} = 2^{20} = 1 \text{ M}$$



Second part

- A computer system has 32-bit addresses and a page size of 4 kilobytes.
- How many bits of the virtual address will remain ***unchanged*** during the address translation process?



Solution

- A computer system has 32-bit addresses and a page size of 4 kilobytes.
- How many bits of the virtual address will remain *unchanged* during the address translation process?
 - Since the page size is $4 \text{ KB} = 2^{12} \text{ B}$, the 12 least significant bits of the virtual address will remain unchanged.



Problem

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.
 - How many bits of the virtual address will remain ***unchanged*** by the address translation process?
 - What is the size of a page table?
 - How many page frames are there in main memory?



First part

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.
- How many bits of the virtual address will remain ***unchanged*** by the address translation process?



Solution

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.
- How many bits of the virtual address will remain *unchanged* by the address translation process?
 - Since the page size is $2\text{KB} = 2^{11} \text{ B}$, the 11 least significant bits of the virtual address will remain unchanged



Second part

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.
 - What is the size of a page table?



Solution

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.

- What is the size of a page table?

- We divide the size of the virtual address space by the page size:

$$4\text{GB}/2\text{KB} = 2^{32}/2^{11} = 2^{21} \text{ entries or}$$

$$2^{21} \times 4 \text{ B} = 2^{23} \text{ B} = 8 \text{ MB}$$



Third part

- A virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2KB. Each page table entry occupies 4 bytes.
 - How many page frames are there in main memory?



Solution

- An old virtual memory system has 512 MB of main memory, a virtual address space of 4 GB and a page size of 2 KB. Each page table entry occupies 4 bytes.
- How many page frames are there in main memory?
 - We divide the size of the main memory by the page size:
 $512 \text{ MB} / 2 \text{ KB} = 2^{29} / 2^{11} = 2^{18} = 256 \text{ K page frames.}$



Problem

- Given the following page reference string

0 1 1 0 1 1 0 0 2 0

and a very small memory that can only accommodate two pages, how many page faults will occur if the memory is managed

- A. By a FIFO policy
- B. By an LRU policy



Answer (I)

- Given the following page reference string

0 1 1 0 1 1 0 0 2 0

and a very small memory that can only accommodate two pages, the FIFO policy will cause four page faults

- Fetch page 0
- Fetch page 1
- Fetch page 2 and expel page 0
- Fetch again page 0 and expel page 1

Answer (II)

- Given the following page reference string

0 1 1 0 1 1 0 0 2 0

and a very small memory that can only accommodate two pages, the LRU policy will cause *three* page faults

- Fetch page 0
- Fetch page 1
- Fetch page 2 and expel page 1



More review questions



True or false

- A computer will never have a page referenced bit **and** a missing bit
- The dirty bit indicates whether a page has been recently accessed
- A page fault rate of one page fault per one thousand references is a good page fault rate
- A TLB miss rate of one miss per one thousand references is a good miss rate



Solution (I)

- A computer will never have a page referenced bit **and** a missing bit **FALSE**
- The dirty bit indicates whether a page has been recently accessed
- A page fault rate of one page fault per one thousand references is a good page fault rate
- A TLB miss rate of one miss per one thousand references is a good miss rate



Solution (II)

- A computer will never have a page referenced bit **and** a missing bit **FALSE**
- The dirty bit indicates whether a page has been recently accessed **FALSE**
- A page fault rate of one page fault per one thousand references is a good page fault rate
- A TLB miss rate of one miss per one thousand references is a good miss rate



Solution (III)

- A computer will never have a page referenced bit **and** a missing bit **FALSE**
- The dirty bit indicates whether a page has been recently accessed **FALSE**
- A page fault rate of one page fault per one thousand references is a good page fault rate **FALSE**
- A TLB miss rate of one miss per one thousand references is a good miss rate



Solution (IV)

- A computer will never have a page referenced bit **and** a missing bit **FALSE**
- The dirty bit indicates whether a page has been recently accessed **FALSE**
- A page fault rate of one page fault per one thousand references is a good page fault rate **FALSE**
- A TLB miss rate of one miss per one thousand references is a good miss rate **TRUE**



Page table organization

- Which page table organization allows entire page tables to reside in main memory?
- How is it possible?



Answer

- Which page table organization allows entire page tables to reside in main memory?
 - Inverted page tables
- How is it possible?
 - Inverted page tables only keep track of the pages that are present in main memory.



Page Replacement Policies

- Among the five following page replacement policies:
Local LRU, Global LRU, Berkeley Clock, Mach and ***Windows***

Which one(s)

- Support ***real-time processes*** ?
- Simulate a ***page-referenced bit*** ?
- Are partially based on the ***FIFO*** policy ?



First part

- Among the five following page replacement policies:
Local LRU, Global LRU, Berkeley Clock, Mach and Windows
- Which one(s) support real-time processes?



Solution

- Among the five following page replacement policies:

Local LRU, Global LRU, Berkeley Clock, Mach and Windows

- Which one(s) support real-time processes?

- **Windows** because each process has a fixed-size minimum resident set.



Second part

- Among the five following page replacement policies:
Local LRU, Global LRU, Berkeley Clock, Mach and *Windows*
- Which one(s) simulate a *page-referenced bit* ?



Solution

- Among the five following page replacement policies:
Local LRU, Global LRU, Berkeley Clock, Mach and *Windows*
- Which one(s) simulate a *page-referenced bit*?
 - *Berkeley UNIX is the only one.*



Third part

- Among the five following page replacement policies:
- ***Local LRU, Global LRU, Berkeley Clock, Mach and Windows***
 - Which one(s) are partially based on the ***FIFO*** ?



Solution

- Among the five following page replacement policies:
- ***Local LRU, Global LRU, Berkeley Clock, Mach and Windows***
- Which one(s) are partially based on the ***FIFO*** ?
 - ***Mach and Windows.***



Page Replacement Policies

- Give examples of
 - Very bad page replacement policies?
 - Policies that are too costly to implement?
 - Good policies that do not require any hardware support?



Solution (I)

- Give examples of
 - Very bad page replacement policies?
Local FIFO, Global FIFO
 - Policies that are too costly to implement?
 - Good policies that do not require any hardware support?



Solution (II)

- Give examples of
 - Very bad page replacement policies?
Local FIFO, Global FIFO
 - Policies that are too costly to implement?
Local LRU, Global LRU, Working Set
 - Good policies that do not require any hardware support?



Solution (III)

- Give examples of
 - Very bad page replacement policies?
Local FIFO, Global FIFO
 - Policies that are too costly to implement?
Local LRU, Global LRU, Working Set
 - Good policies that do not require any hardware support?
Mach, Berkeley Clock, Windows